

Theoretical approaches to cosmic tensions

Tanvi Karwal



CosmoVerse@Kraków

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Based on work with: Kim Berghaus, Vivian Poulin, Tristan L. Smith, Marco Raveri, Lucas Secco, Omar Ramadan, Yashvi Patel, Thejs Brinckmann, Marc Kamionkowski, Bhuv Jain, Justin Khoury, Mark Trodden, Daniel Grin, Wayne Hu, Elisabeth Krause, Jeremy Sakstien, Vivian Miranda

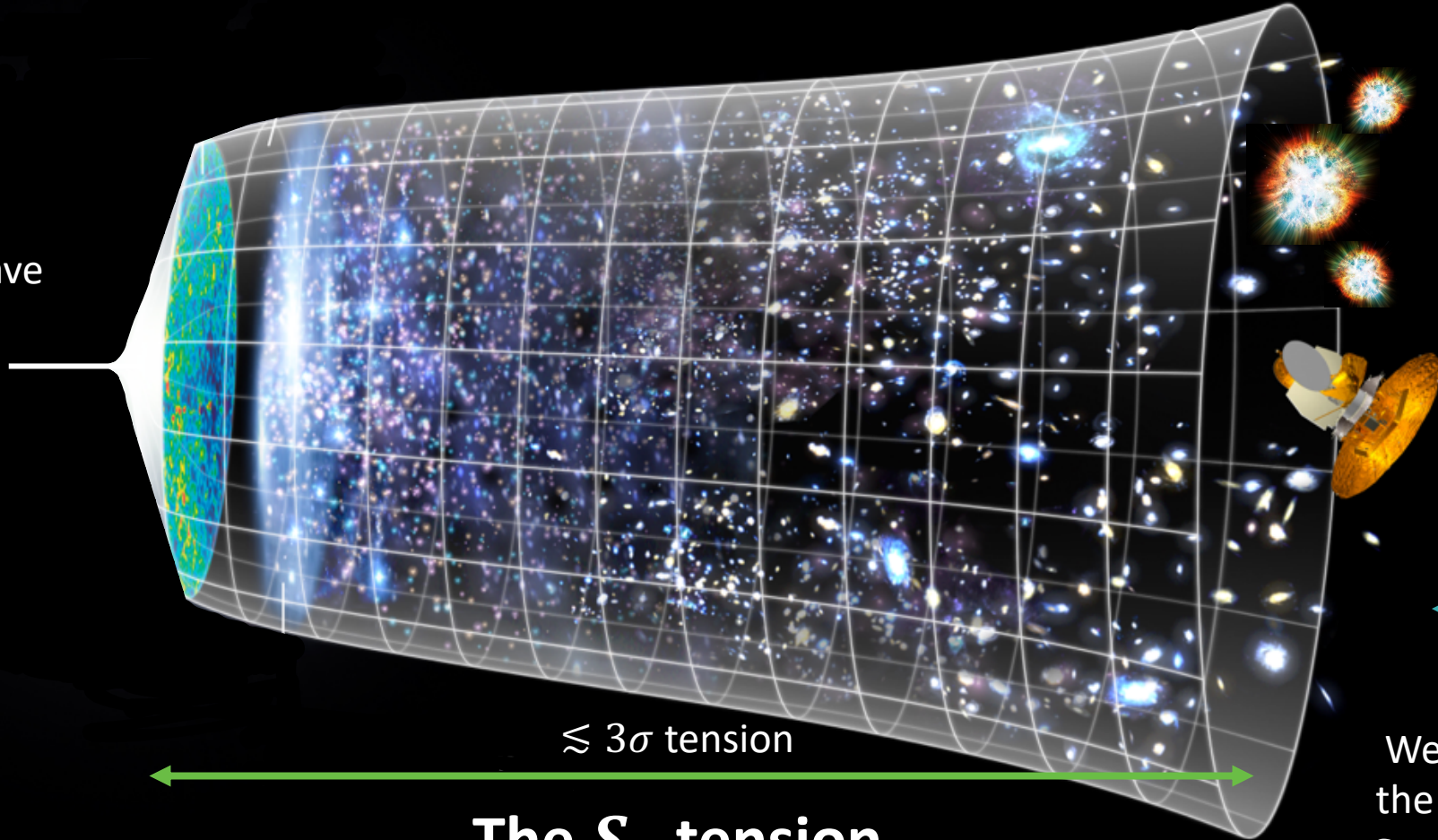
Fit Λ CDM to the CMB
 $H_0 = 67.4 \pm 0.5$
km/s/Mpc

5.7σ tension

Cepheid distance ladder
 $H_0 = 73.29 \pm 0.90$
km/s/Mpc

The Hubble tension

Cosmic microwave
background
+
Cosmological
assumptions



Late universe +
astro/cosmo
assumptions

Fit Λ CDM to the CMB
 $S_8 = 0.832 \pm 0.013$

$\approx 3\sigma$ tension

Weak lensing in
the late universe
 $S_8 = 0.759^{+0.024}_{-0.021}$

The S_8 tension

Cosmic tensions, solutions and extensions

- Guidelines for a theoretical solution to H_0
- The Early Dark Energy solution(s)
- Challenges to EDE solutions
- Going beyond EDE

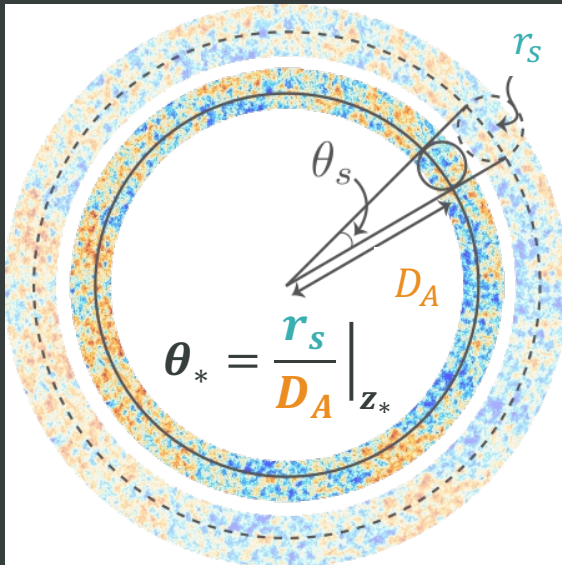
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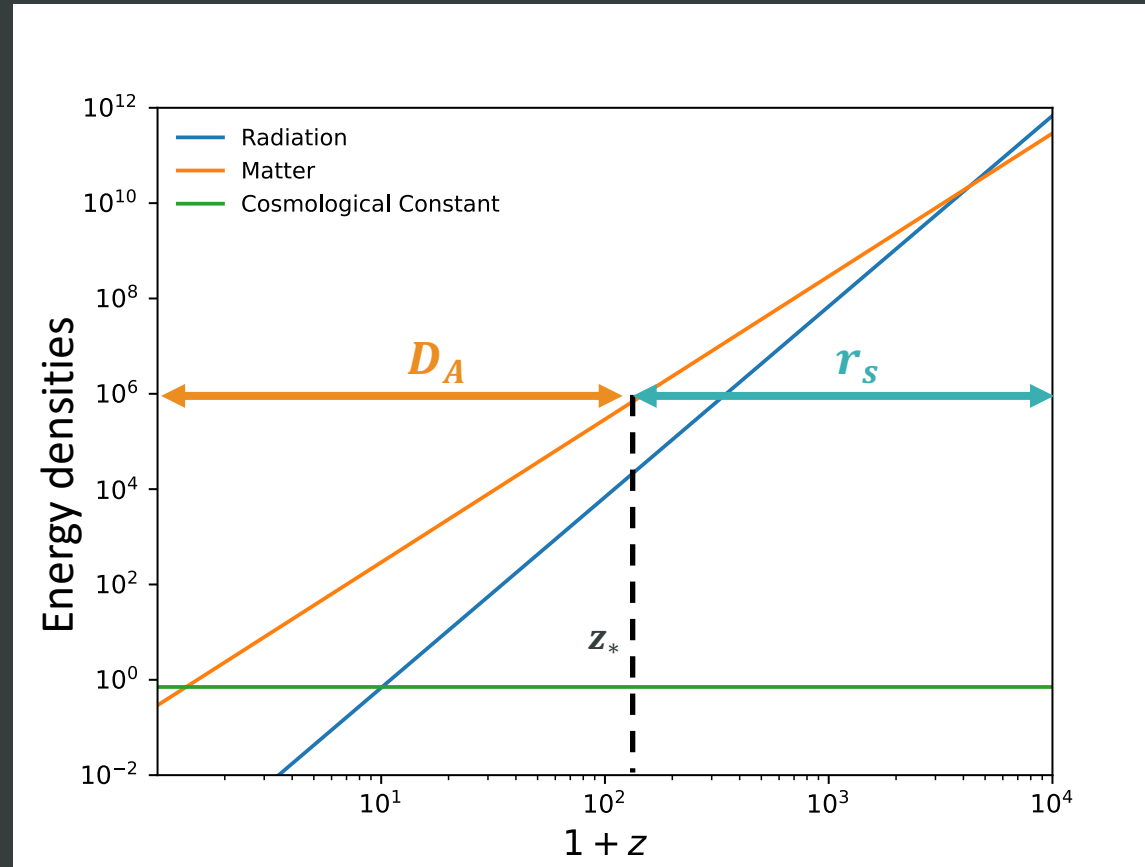
Theoretical guidelines

A model-dependent H_0

Precisely measured θ_* is an approximate proxy for CMB peak locations



Cartoon by Tristan L. Smith



$$D_A \propto 1/H_{post}$$

$$r_s \propto 1/H_{pre}$$

Both are fixed by Λ CDM

For precisely measured θ_*

$$\theta_* \sim \frac{r_s}{1/H_{post}} \sim r_s H_0$$

$$r_s \propto 1/H_0$$

In support of an early universe modification:

Karwal et al [1608.01309]

Planck [1807.06209]

Bernal et al [1607.05617]

Evslin et al [1711.01051]

Aylor et al [1811.00537]

Raveri et al [2002.11707]

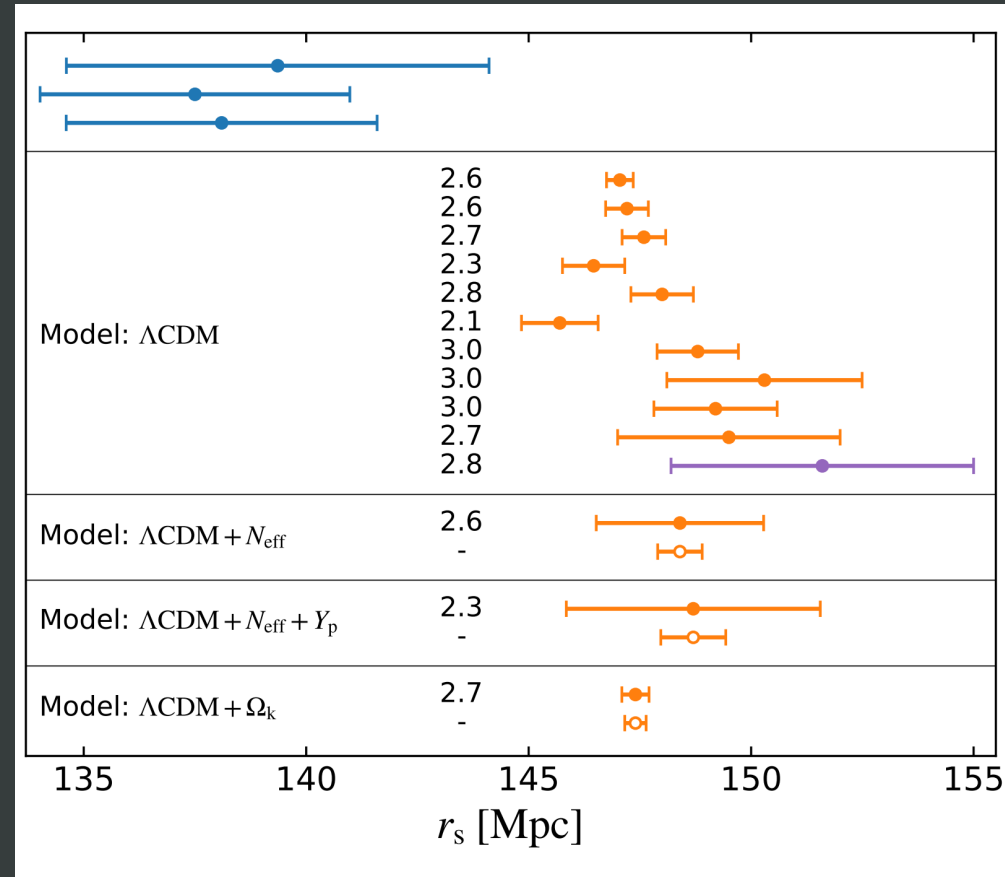
Theoretical guidelines

Hubble Tension \leftrightarrow Sound Horizon Tension

Distance ladder and other late universe

CMB, early universe

No CMB data, early universe



Higher H_0 measured

Lower H_0 inferred

Lower H_0 inferred

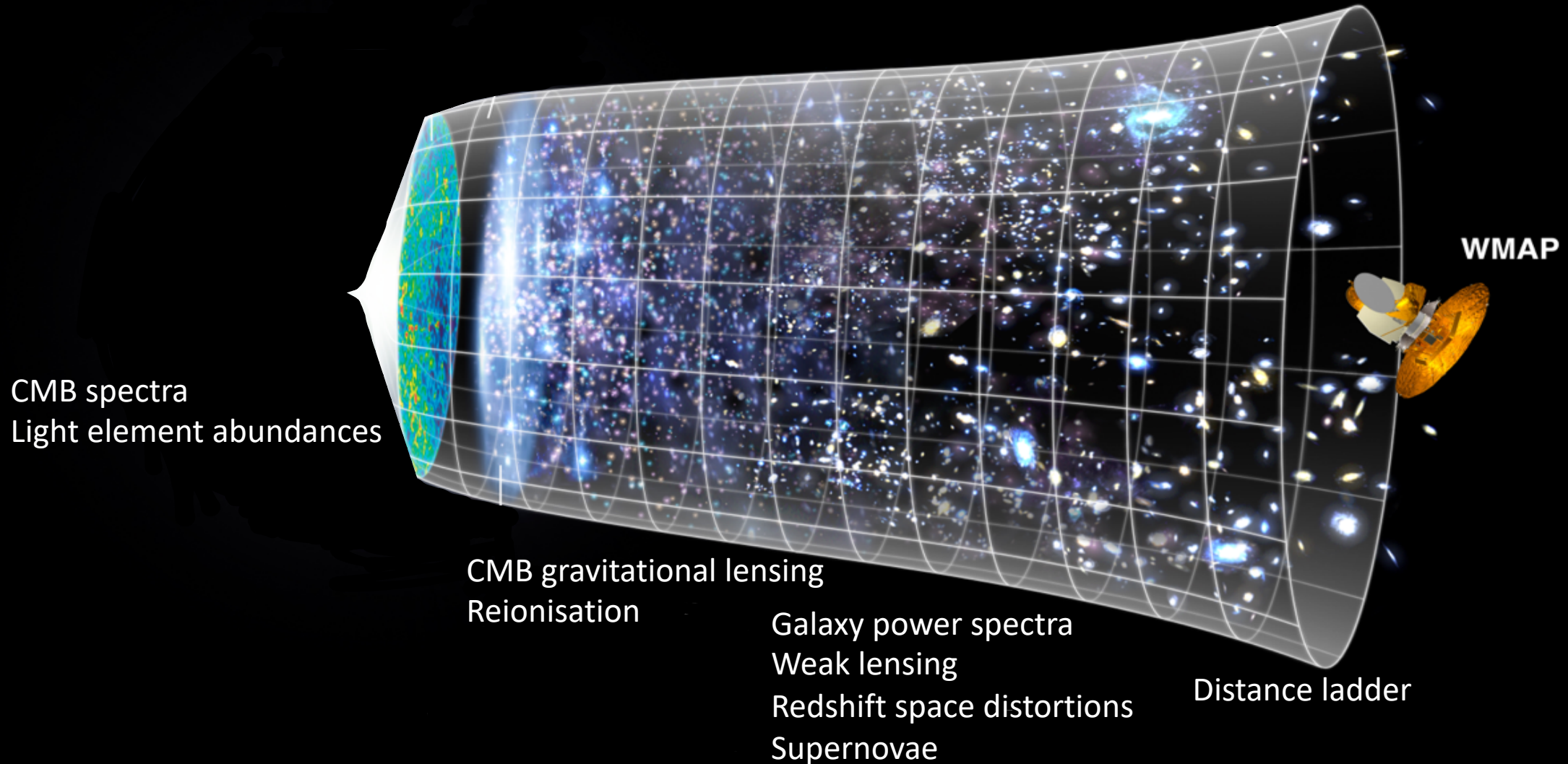
Aylor et al [1811.00537]

Theoretical guidelines

- Maintaining a good fit to the CMB requires $r_s \propto 1/H_0$.
Decrease the sound horizon r_s to increase the predicted H_0 .
Because $r_s \propto 1/H_{pre}(z)$, new physics must be added before the CMB

Theoretical guidelines

Leave late universe unchanged

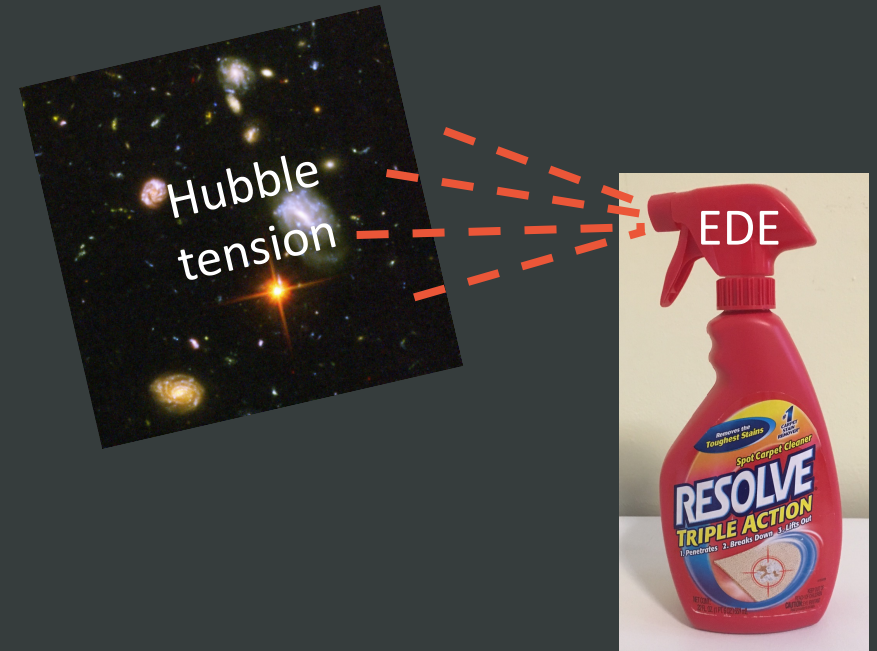


Theoretical guidelines

- Maintaining a good fit to the CMB requires $r_s \propto 1/H_0$.
Decrease the sound horizon r_s to increase the predicted H_0 .
Because $r_s \propto 1/H_{pre}(z)$, new physics must be added before the CMB
- New physics must vanish post recombination
 - Modifications to D_A introduce new tensions between CMB and BAO
 - DESI and SNe may prefer $w(z)$ CDM but these do not increase H_0
 - Very-late $H(z)$ modifications do not resolve the tension at $z \simeq 0.15$

Cosmic tensions, solutions and extensions

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Early dark energy

Effect on cosmic microwave background

Farthest distance that
sound waves travelled

$$\sim r_s \sim \theta_*$$

Electrons and protons
have to combine
sooner

The Universe must expand faster than Λ CDM at very early times, before the CMB was emitted

Sound waves travel a
shorter distance if CMB is
emitted earlier

The Universe
has to cool through
expansion faster

WMAP, NASA

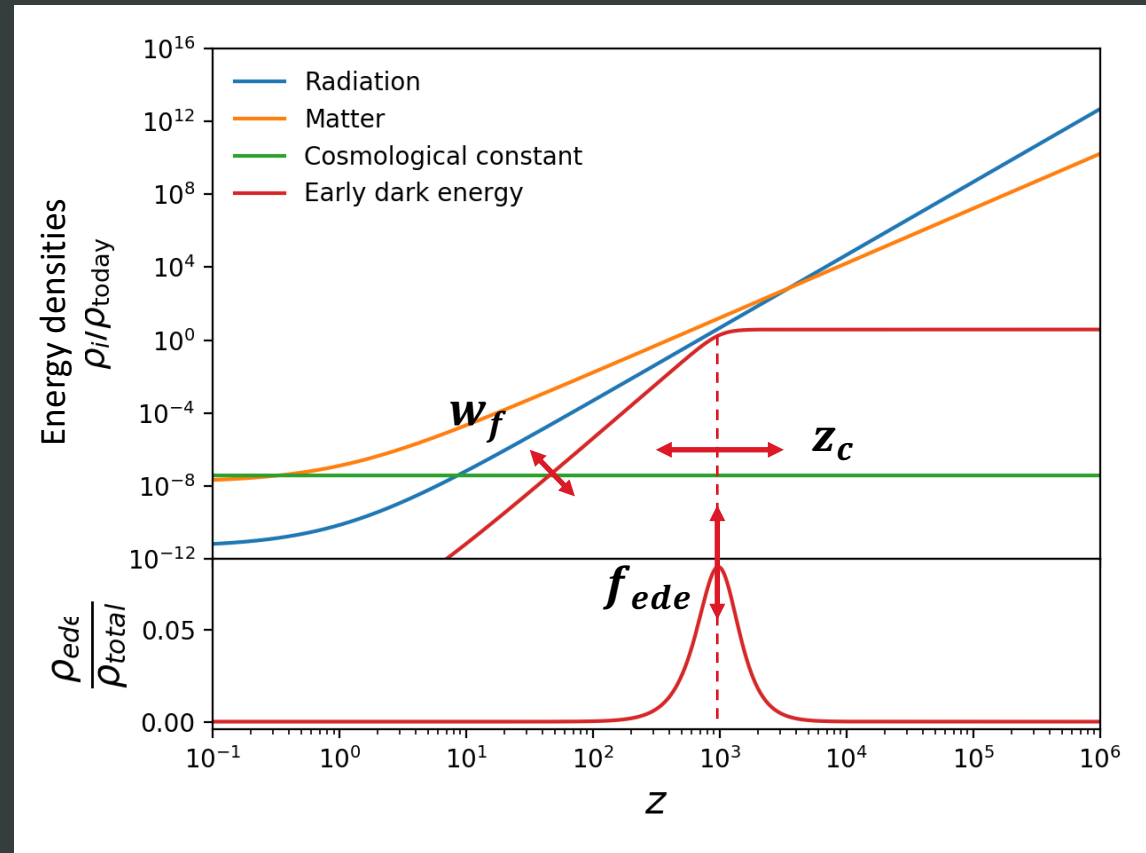
Early dark energy Phenomenology

$H^2 \sim \rho_{total}$
Expansion rate \sim energy content

Additional energy component with the properties:

- Λ -like behaviour initially
- Then dilutes faster than matter at w_f
- Localised peak in $f_{ede} = \frac{\rho_{ede}}{\rho_{total}}$ at z_c

f_{ede} - how much EDE
 z_c - when EDE appears
 w_f - how fast it disappears



Theoretical guidelines

- ✓ Decrease the sound horizon r_s to increase the predicted H_0 .
Because $r_s \propto 1/H_{pre}(z)$, new physics must be added before the CMB
- ✓ New physics must vanish post recombination

Early dark energy Models

- Early Dark Energy, the Hubble Parameter, and the String Axiverse
TK & Kamionkowski [1608.01309]
- Cosmological Implications of Ultralight Axionlike Fields
Poulin, TK et al [1806.10608]
- Early Dark Energy Can Resolve The Hubble Tension
Poulin, TK et al [1811.04083]
- Thermal Friction as a Solution to the Hubble Tension
Berghaus & TK [1911.06281]
- Chameleon Early Dark Energy and the Hubble Tension
TK, Raveri, Jain, Khoury, Trodden [2106.13290]
- Thermal Friction as a Solution to the Hubble and Large-Scale Structure Tensions
Berghaus & TK [2204.09133]
- An Attractive Proposal for Resolving the Hubble Tension: Dynamical Attractors that Unify Early and Late Dark Energy
Ramadan, TK & Sakstein [2309.08082]

Non-comprehensive list:

- Rock 'n' Roll Solutions to the Hubble Tension. Agrawal et al [1904.01016]
- Axion-Dilaton Destabilization and the Hubble Tension. Alexander & McDonough [1904.08912]
- Acoustic Dark Energy: Potential Conversion of the Hubble Tension. Lin, Raveri, Hu [1905.12618]
- Oscillating scalar fields and the Hubble tension: a resolution with novel signatures. Smith, Poulin, Amin [1908.06995]
- New Early Dark Energy. Neidermann & Sloth [1910.10739]
- Early Dark Energy from Massive Neutrinos as a Natural Resolution of the Hubble Tension. Sakstein & Trodden [1911.11760]
- Unifying Inflation with Early and Late-time Dark Energy in F(R) Gravity. Nojiri et al [1912.13128]
- Is the Hubble tension a hint of AdS phase around recombination? Ye & Piao [2001.02451]
- Unified framework for early dark energy from α -attractors. Braglia et al [2005.14053]
- A novel early Dark Energy model. Garcia, Castaneda, Tejeiro [2009.07357]
- Neutrino-Assisted Early Dark Energy: Theory and Cosmology. Gonzalez et al [2011.09895]
- The Early Dark Sector, the Hubble Tension, and the Swampland. McDonough, .. Hill, Hu, et al [2112.09128]
- Effects of a Geometrically Realized Early Dark Energy Era on the Spectrum of Primordial Gravitational Waves, Oikonomou et al [2206.00721]
- Early dark energy and the screening mechanism, Sadjadi et al [2205.15693]
- Early Dark Energy from a Higher-dimensional Gauge Theory, Kojima et al [2205.13777]
- Unifying inflation with early and late dark energy with multiple fields: Spontaneously broken scale invariant two measures theory, Guendelman et al [2201.06470]

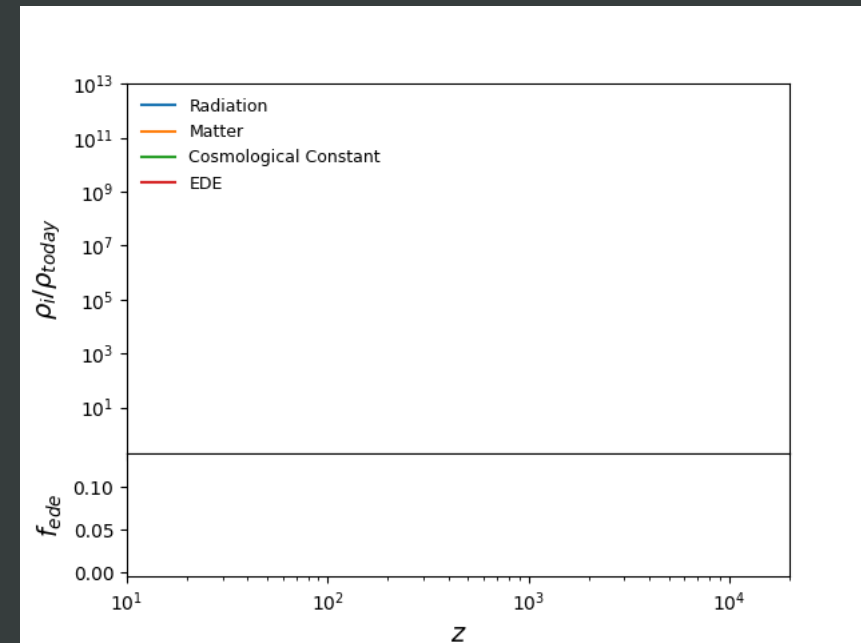
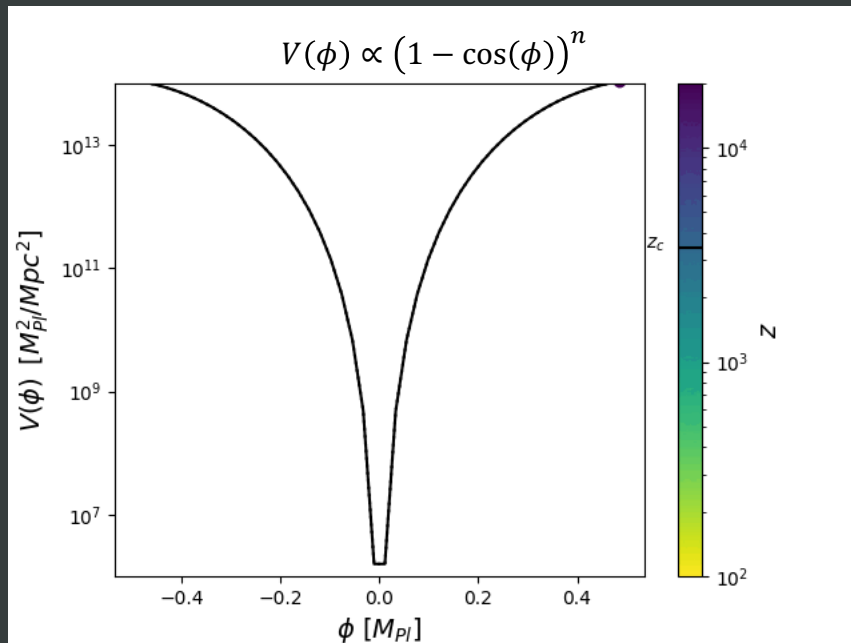
EDE@Krakow

William Giarè - Inflation and the Hubble Tension talk

Joby Kochappan – EDE birefringence poster

Early dark energy

Ultra-light-axion-inspired scalar potential



Based on Poulin,.. [TK](#), et al [arxiv:1806.10608]

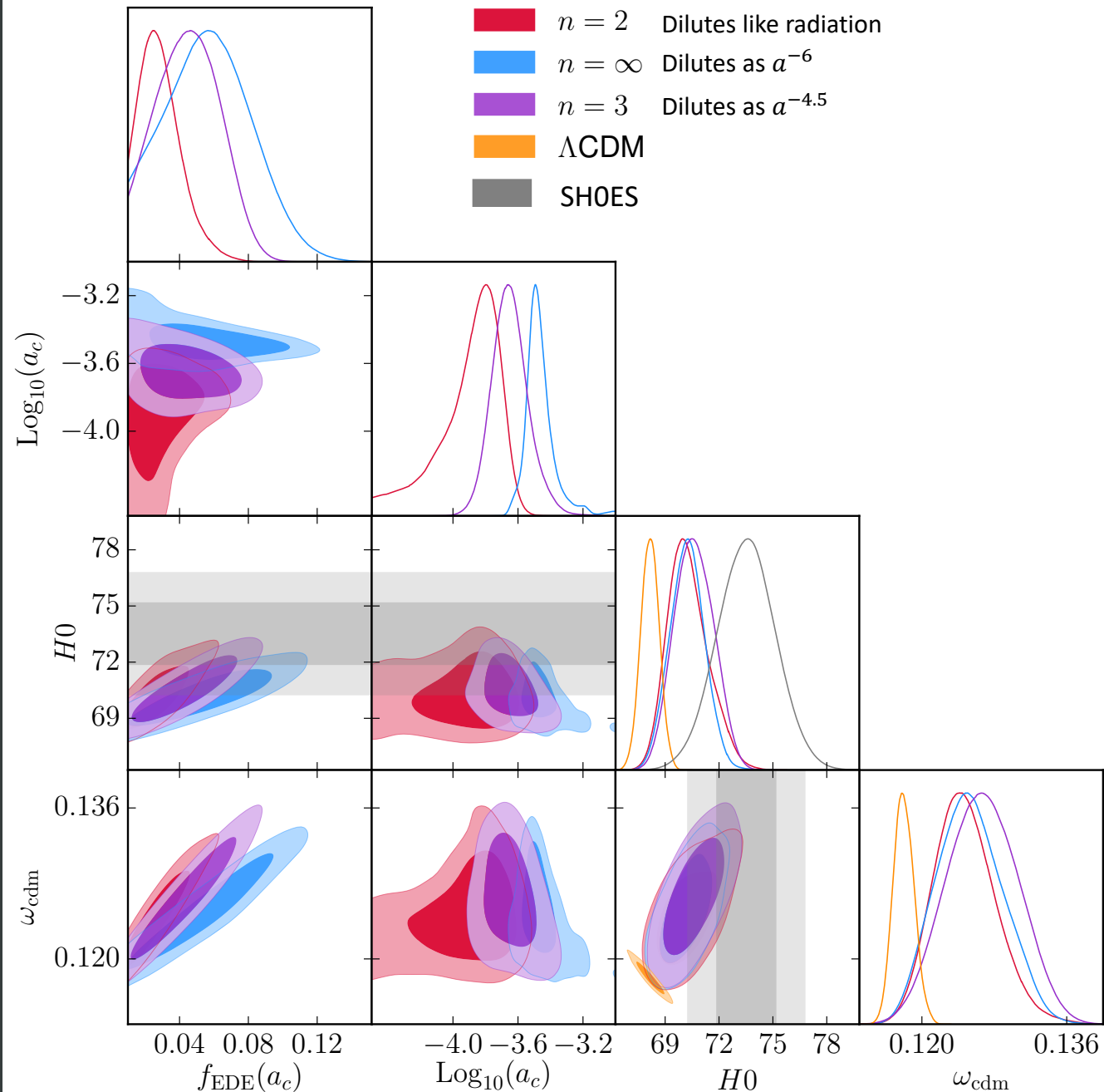
Early dark energy ULA-inspired scalar

Fit to CMB+BAO+SNe+H0

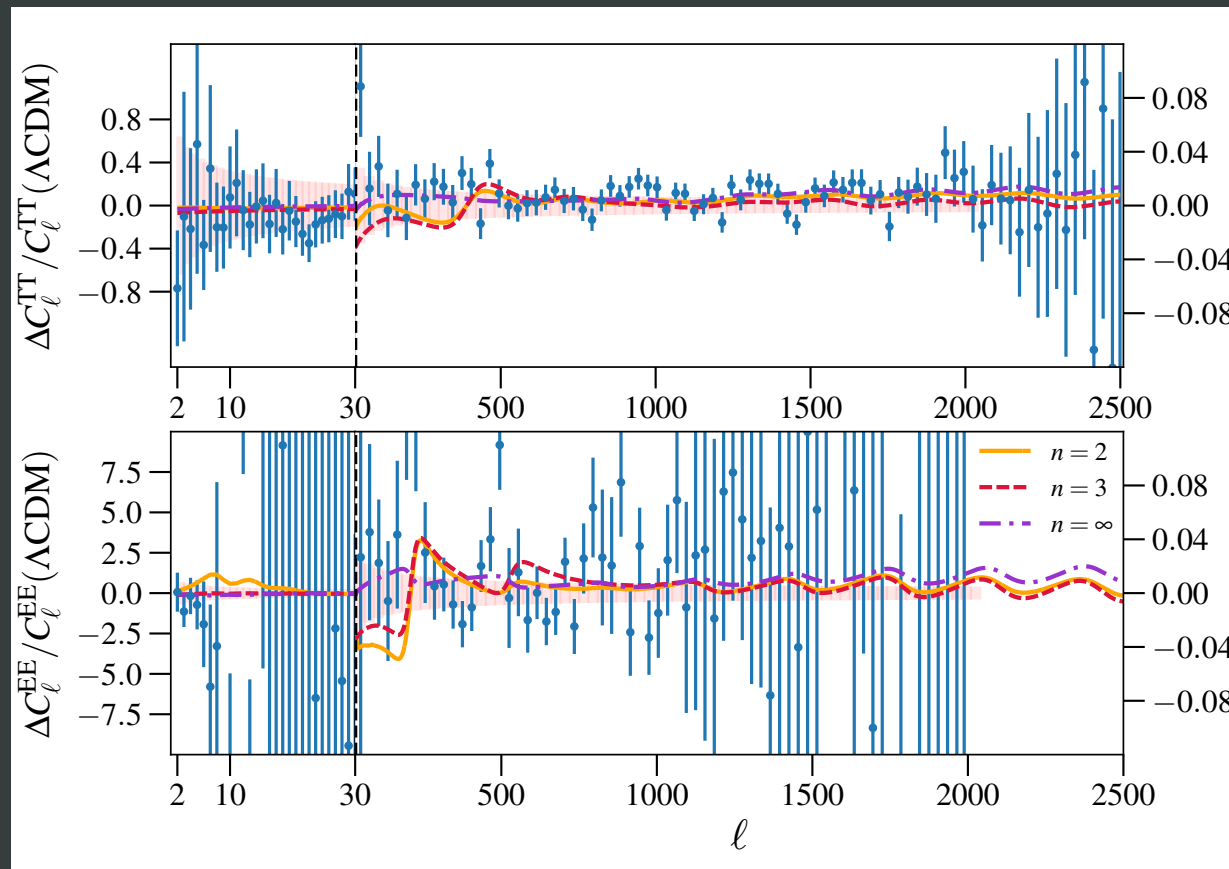
- ω_{cdm} = amount of cold dark matter today
- $f_{ede}(a_c)$ = fractional energy density in the axion field at critical redshift $z_c \approx 1/a_c$
- $w_f = \frac{n-1}{n+1}$

We find an improved χ^2 for Λ CDM + EDE for combined datasets

Poulin,.. TK et al [1811.04083]



Early dark energy Detection in the CMB



Poulin, TK et al [1811.04083]

Could detect EDE in
cosmic-variance-limited,
high- ℓ
CMB polarisation data

ACT and SPT have already
had implications for EDE
constraints

Smith et al [2309.03265]
Smith et al [2202.09379]
La Posta et al [2112.10754]
Hill et al [2109.04451]
Lin et al [2009.08974]
Chudaykin et al [2004.13046]
and [2011.04682]

Cosmic tensions, solutions and extensions

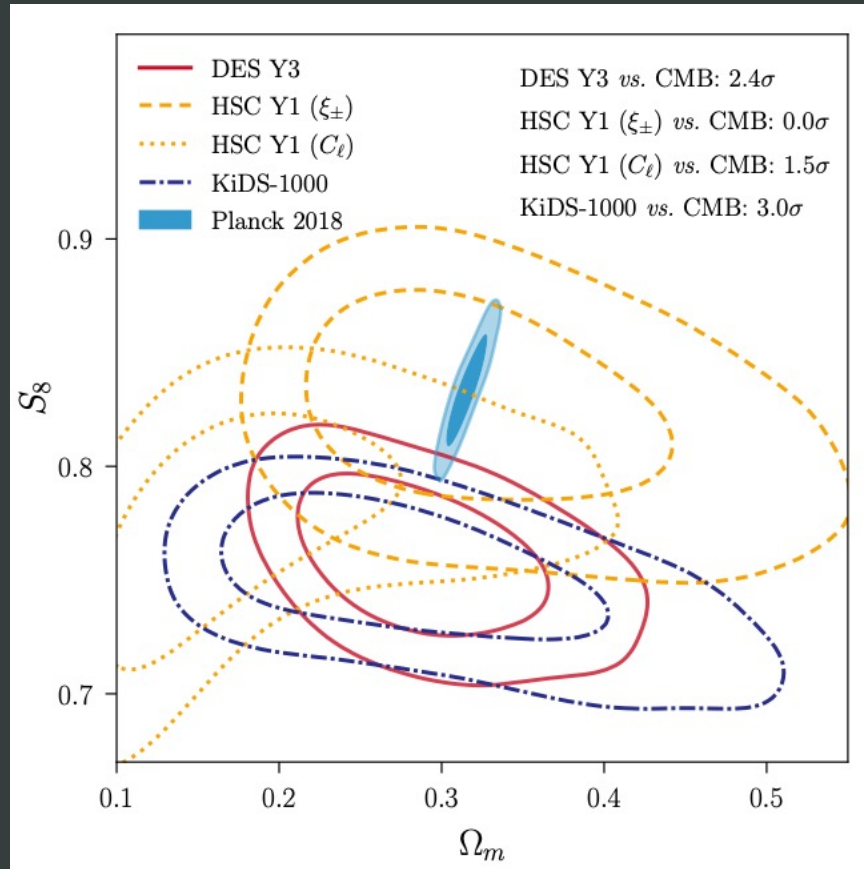
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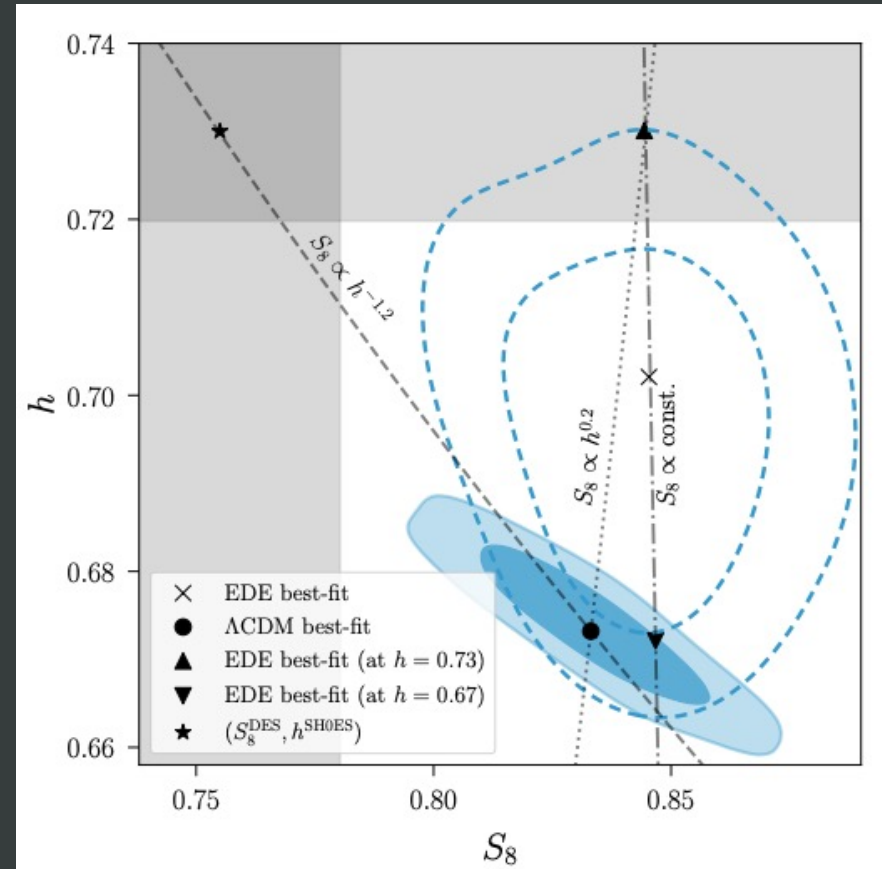
Challenges to EDE

Weak-lensing S_8 tension

Amplitude σ_8 of matter density fluctuations
 $S_8 = \sigma_8 \sqrt{\Omega_m} / 0.3$



Impact of EDE on WL tension



Secco, TK et al [2209.12997]

Challenges to EDE

Solutions and obstacles

- Resolves the Hubble tension
- Can arise from numerous theoretical scenarios
- Scalar field $V(\phi) \sim (1 - \cos \phi)^n$ does particularly well
- Improves the fit to cosmological data relative to Λ CDM
- Worsens the WL tension
- Solution is fine-tuned in theoretical parameters – why matter-radiation equality?
- $V(\phi) \sim (1 - \cos \phi)^n$ is a very contrived potential
- Need to include local H_0 while fitting via Bayesian methods

Cosmic tensions, solutions and extensions

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Beyond EDE

EDE without SH_0 ES priors

Alternate statistical frameworks

Bayesian inference

$$\mathcal{P}(\theta|d) = \frac{\Pi(\theta)\mathcal{L}(d|\theta)}{\mathcal{E}(d)}$$

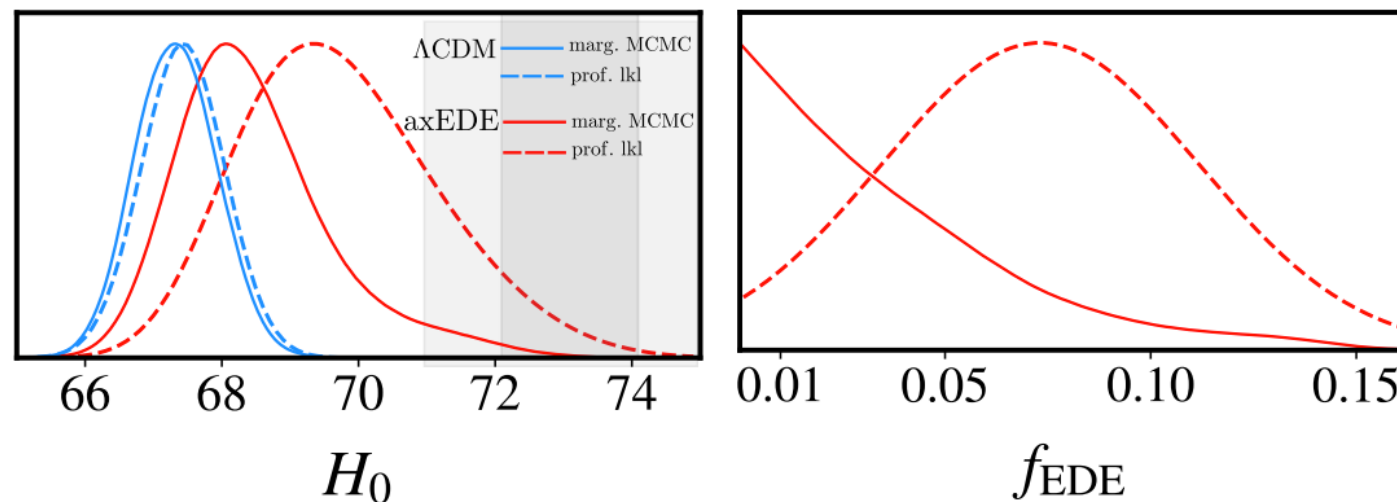
Prior volume increases as $f_{ede} \rightarrow 0$
 z_c and w_f become unconstrained

Profile likelihoods

No dependence on prior

$$\mathbb{P}(\theta_i) = \max \mathcal{L}(\theta|\theta_i = \theta'_i) \forall \theta'_i$$

Fit to CMB+BAO+SNe,
no H_0 prior



Poulin, Smith and TK [2302.09032]

Beyond EDE

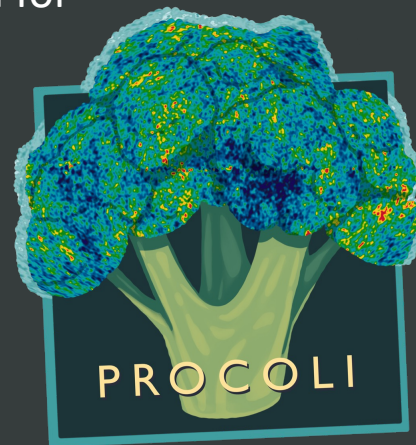
Profile likelihoods

Profile likelihoods

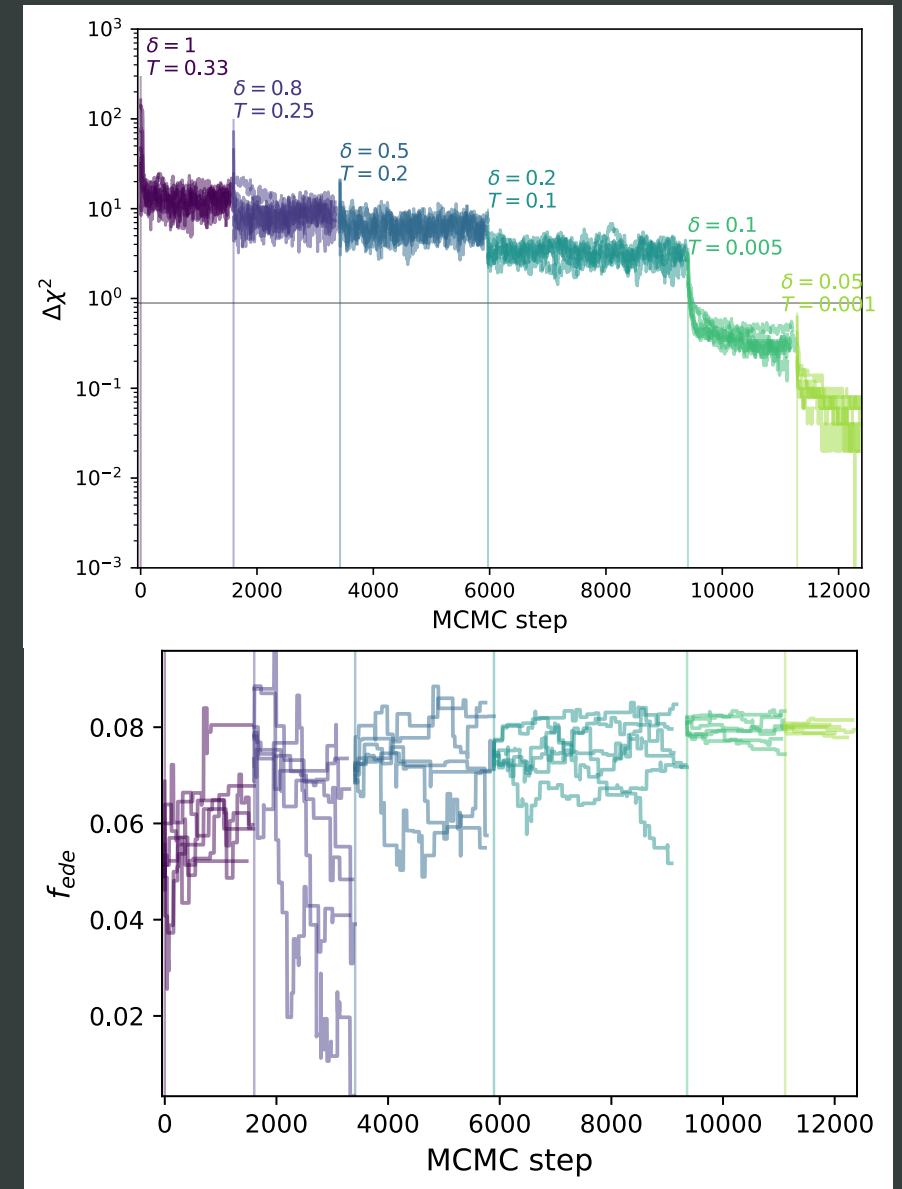
No dependence on prior

$$\mathbb{P}(\theta_i) = \max_{\theta} \mathcal{L}(\theta | \theta_i = \theta'_i) \forall \theta'_i$$

With simulated-annealing optimization for high-dimensional parameter spaces



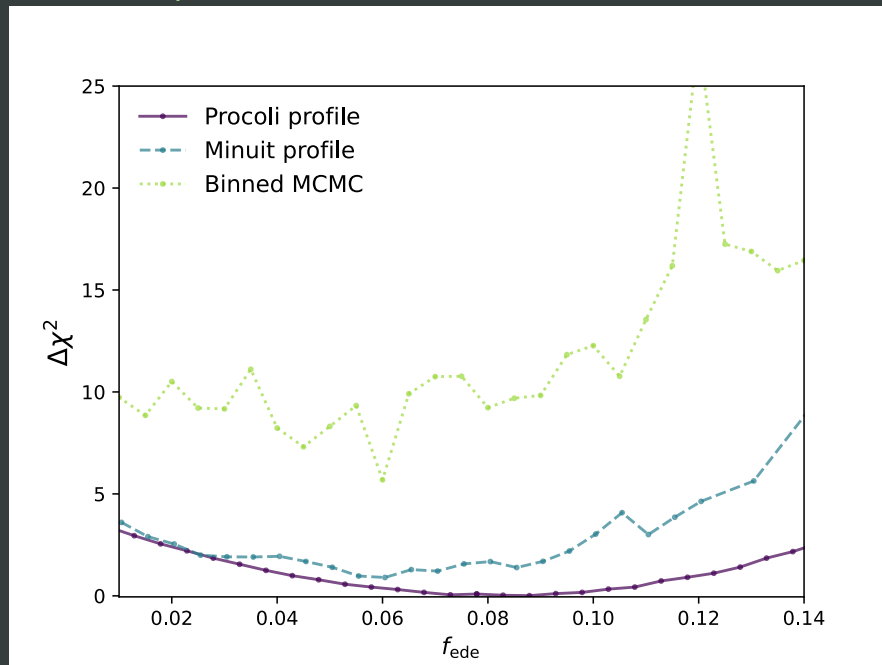
TK et al [2401.14225]



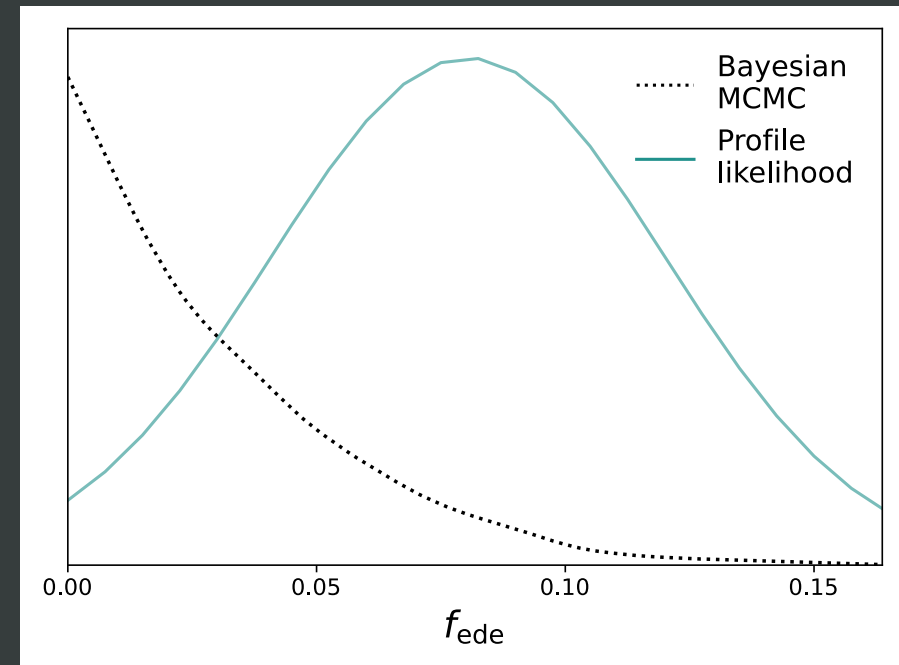
Beyond EDE

Profile likelihoods

Profile likelihood with simulated annealing
Profile likelihood without stochastic algorithm
Posterior profile



Additional insight into model that may be hidden by prior-dependent posteriors



TK et al [2401.14225]

Challenges to EDE

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Beyond EDE

Chameleon EDE coupled to dark matter

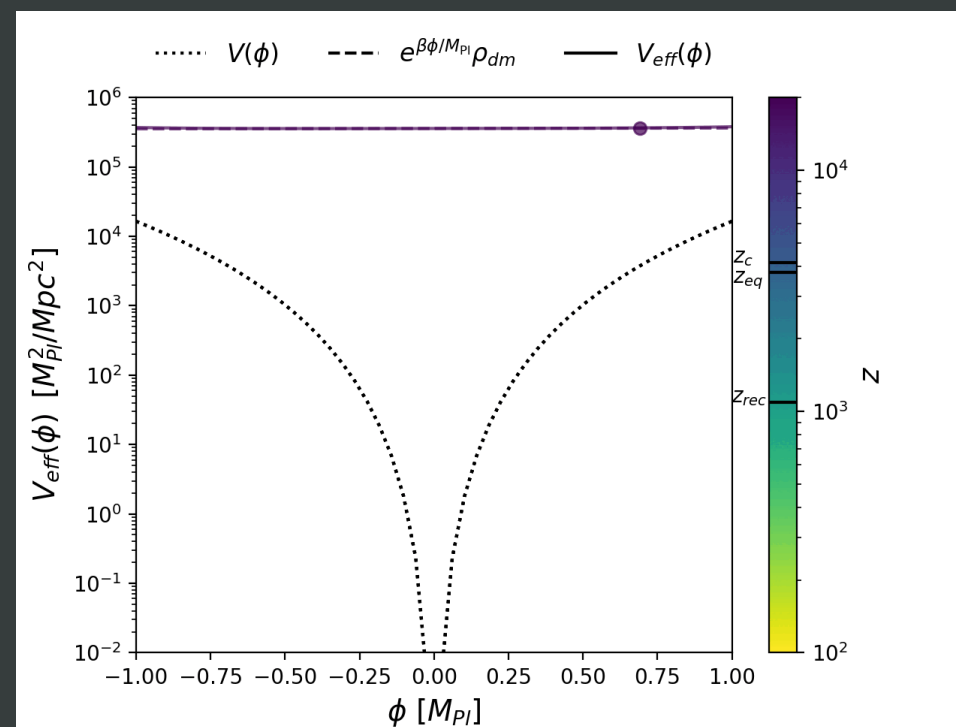
Conformally couple a scalar field to dark matter

$$\rho_{total} += \rho_{dm}A(\phi)$$

$$V_{eff}(\phi) = V(\phi) + \rho_{dm}A(\phi)$$

- Modifies DM evolution $\rightarrow S_8$?
- Tie the redshift of EDE to z_{eq} through coupling $A(\phi)$

$$V(\phi) \sim \phi^4 \quad A(\phi) \sim e^{\beta\phi}$$



TK et al [2106.13290]

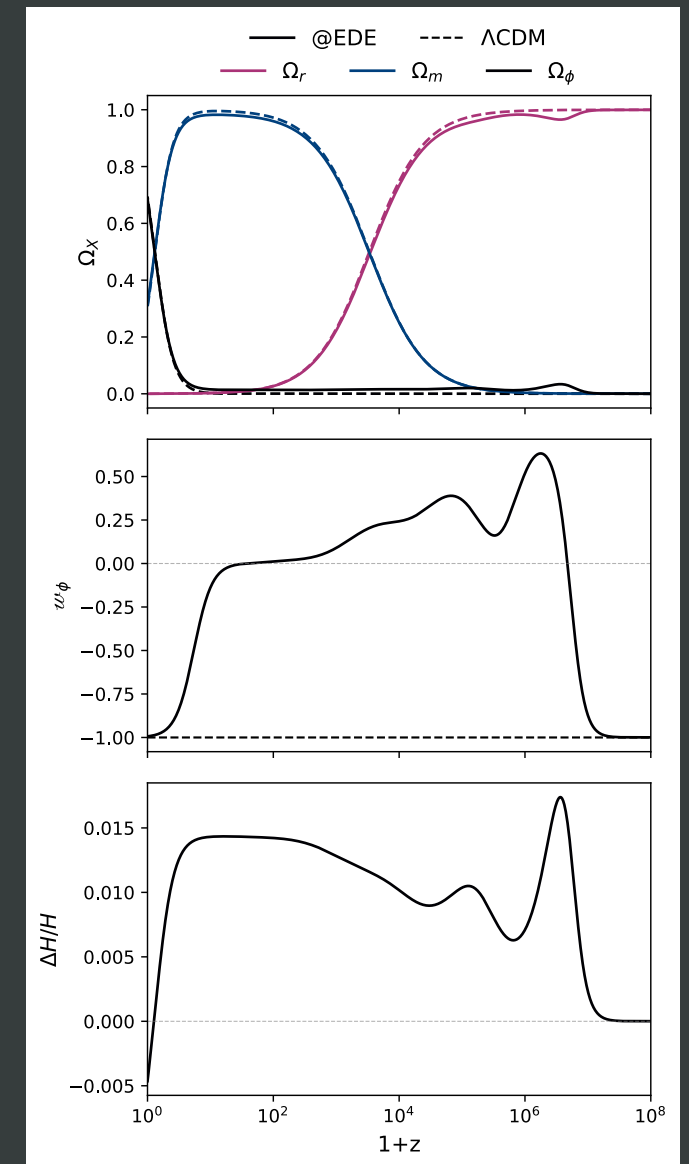
Beyond EDE

Attractive EDE coupled to dark energy

$$V(\phi) = V_\alpha e^{-\alpha \frac{\phi}{M_{Pl}}} + V_\beta e^{-\beta \frac{\phi}{M_{Pl}}}$$

For $\alpha > \beta$, early and late dark energy attractors

- EDE saddle point in the radiation era
- Transition to a matter saddle in the matter era
- Settle into dark energy attractor



Ramadan, TK et al [2309.08082]

Beyond EDE

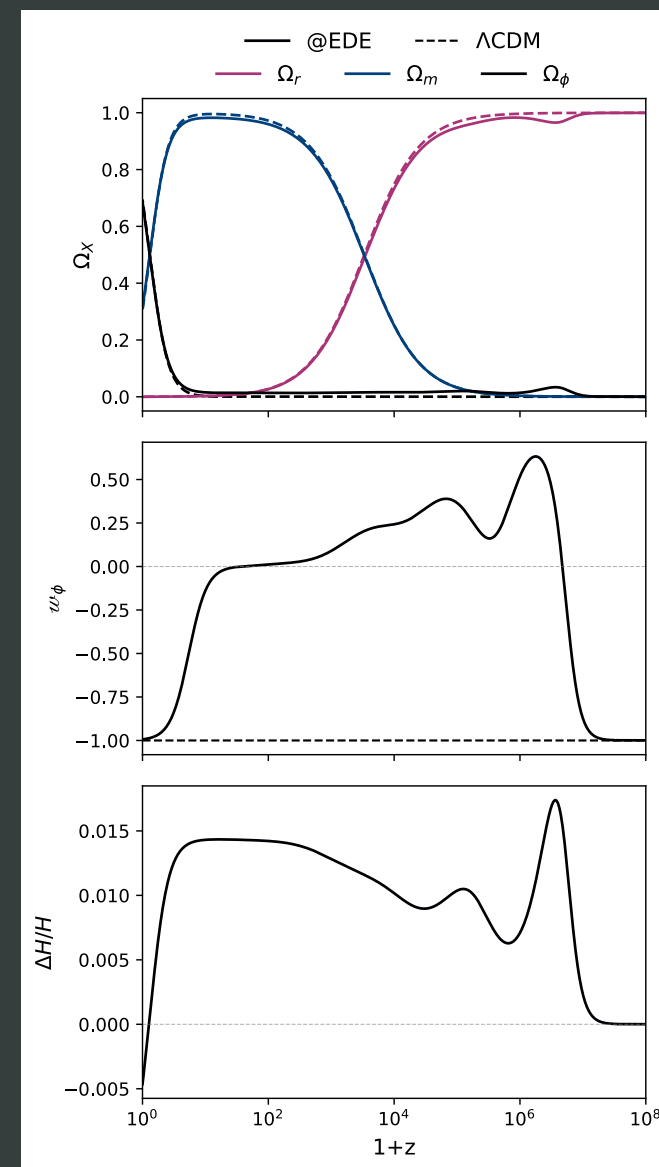
Attractive EDE coupled to dark energy

$$V(\phi) = V_\alpha e^{-\alpha \frac{\phi}{M_{Pl}}} + V_\beta e^{-\beta \frac{\phi}{M_{Pl}}}$$

Too much contribution from @EDE during the matter era strongly constrains this model, preventing a Hubble solution

- @EDE presence at early times increases the early ISW effect, requiring an increase in ω_c
- @EDE contribution post-recombination decreases D_A requiring a decrease in ω_c

Model-building guidance - minimise the contribution of @EDE during matter-domination



Ramadan, TK et al [2309.08082]

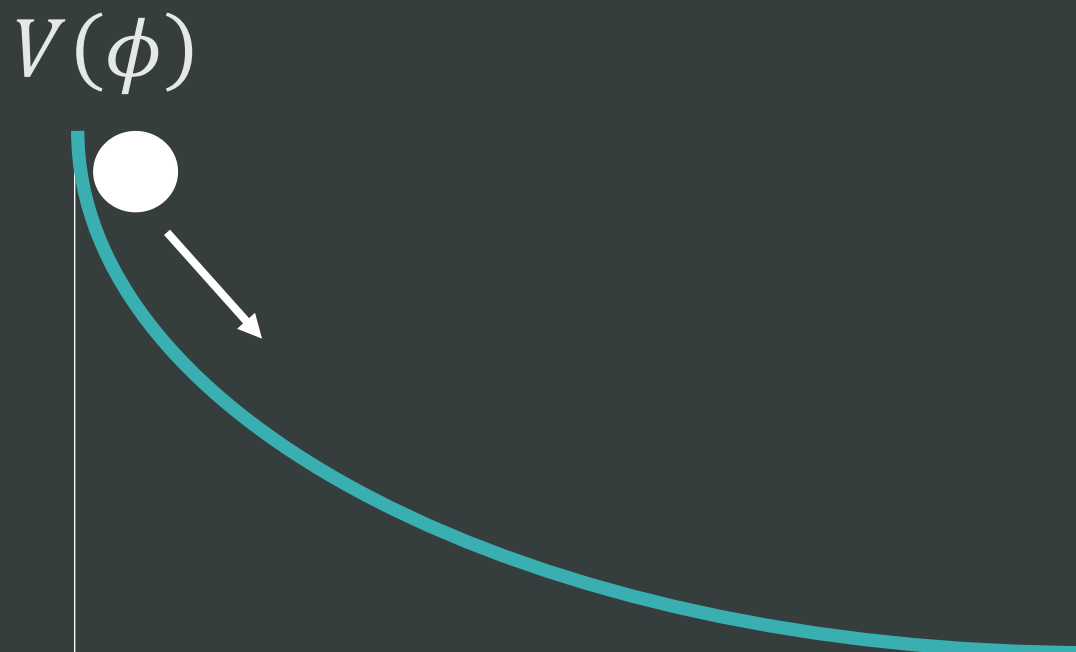
Beyond EDE

Dissipative axion EDE coupled to dark radiation

Uncoupled scalar experiences **Hubble friction**. Uncoupled DR dilutes as $(1+z)^4$

$$\ddot{\phi} + (3H)\dot{\phi} + V_{\phi} = 0$$

$$\dot{\rho}_{dr} = -4H\rho_{dr}$$



Berghaus & Karwal [1911.06281]

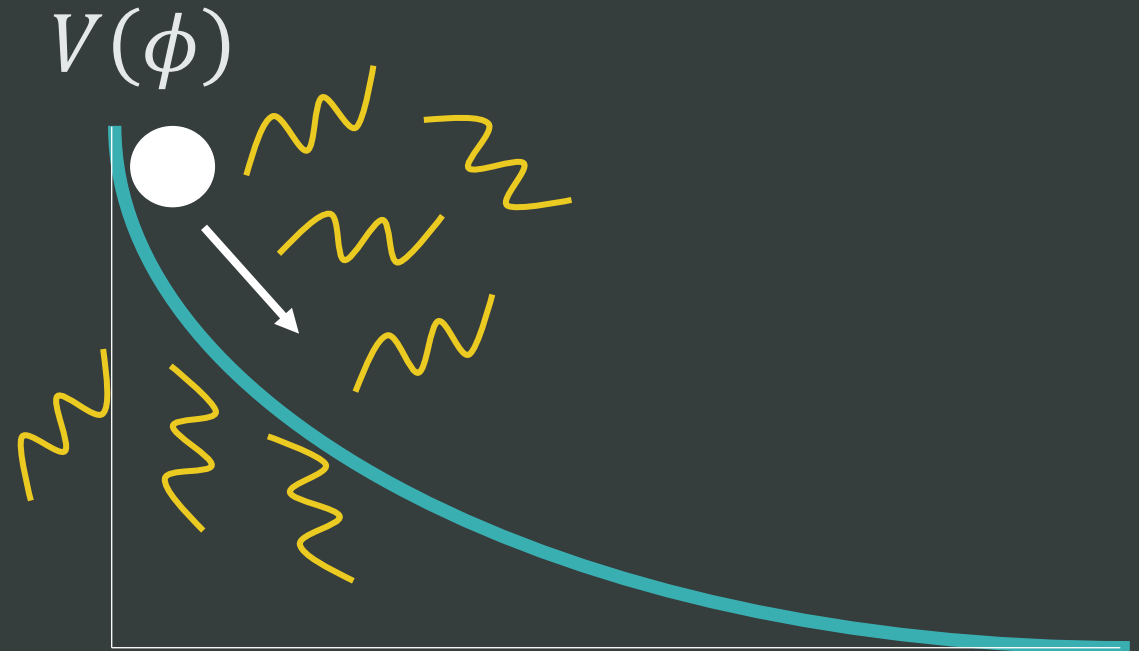
Beyond EDE

Dissipative axion EDE coupled to dark radiation

Scalar coupled to DR **additionally**
experiences **thermal friction**

$$\ddot{\phi} + (3H + \Upsilon) \dot{\phi} + V_{\phi} = 0$$

$$\dot{\rho}_{dr} = -4H\rho_{dr} + \Upsilon\dot{\phi}^2$$



Berghaus & Karwal [1911.06281]

Beyond EDE

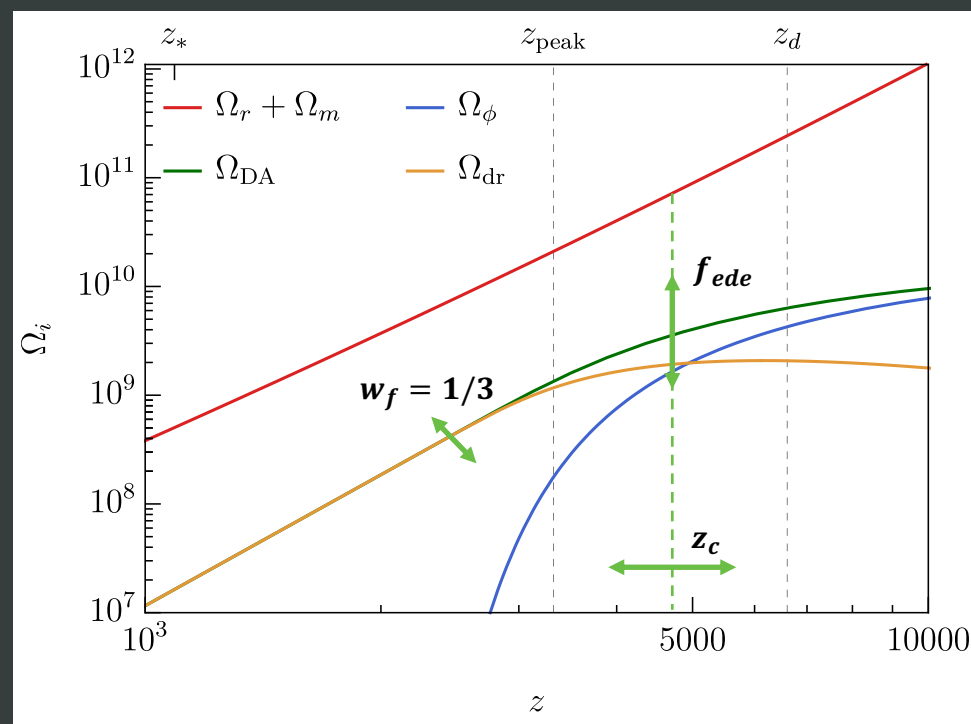
Dissipative axion EDE coupled to dark radiation

$$\ddot{\phi} + (3H + \Upsilon(T_{dr})) \dot{\phi} + V_{\phi} = 0$$

$$\dot{\rho}_{dr} = -4H\rho_{dr} + \Upsilon(T_{dr})\dot{\phi}^2$$

$$\begin{aligned} m, \phi_i &\rightarrow f_{ede} \\ m, \Upsilon(T_{dr}) &\rightarrow z_c \\ w_f &= 1/3 \end{aligned}$$

Robust to choice of $V(\phi)$



Berghaus & Karwal [1911.06281]

Beyond EDE

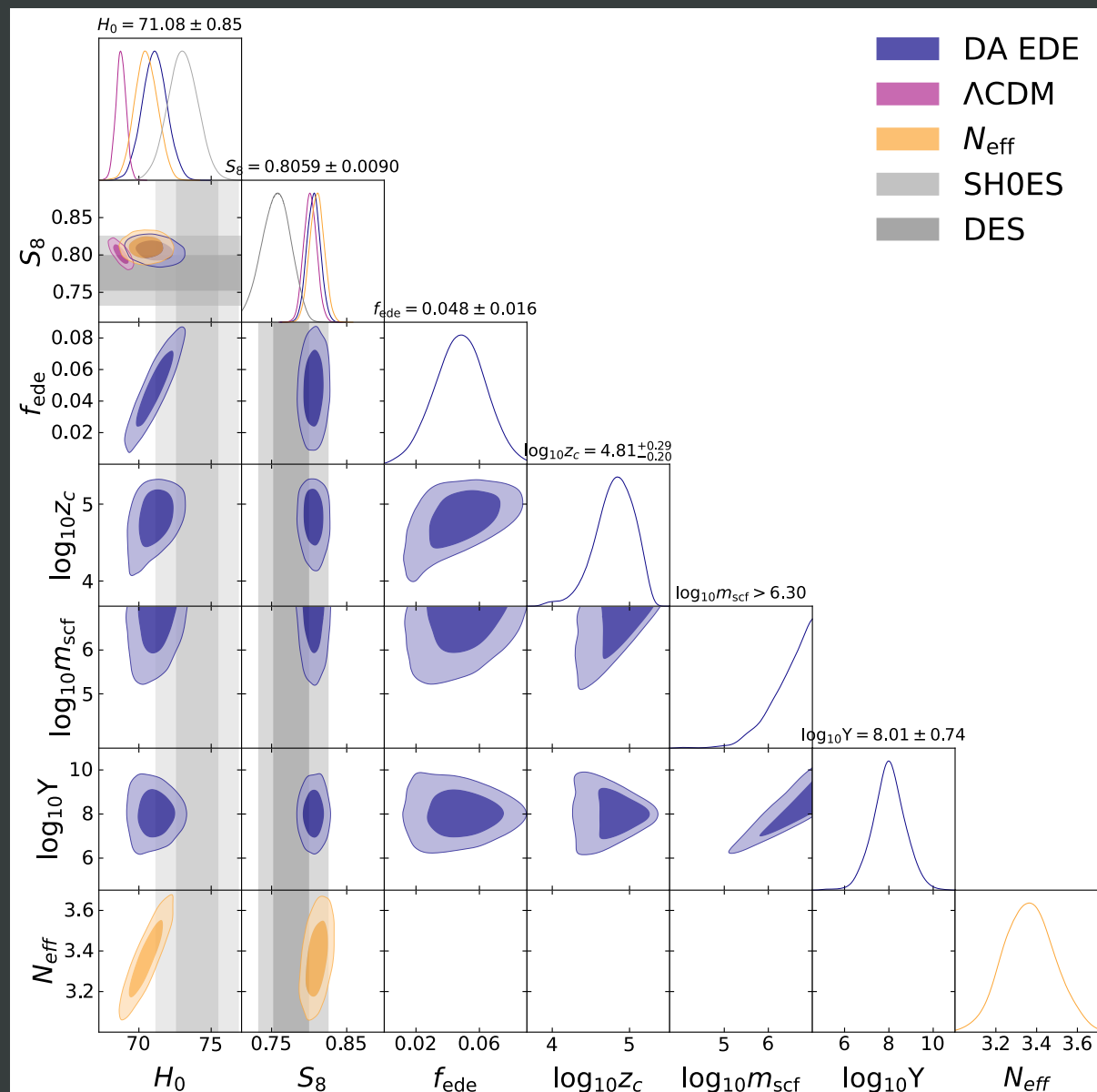
DA EDE coupled to DR

Fit to CMB+BAO+SNe+H0+DES

- Higher Hubble than Λ CDM and N_{eff}
- Similar S_8 to Λ CDM and N_{eff}
- Extra radiation preferred over EDE-like injection
- Similar fit to CMB as Λ CDM, but worse than Λ CDM fit to concordant data

Dissipative axion performs better than N_{eff} but suffers the same CMB constraints as other extra radiation

Berghaus & Karwal [2204.09133]



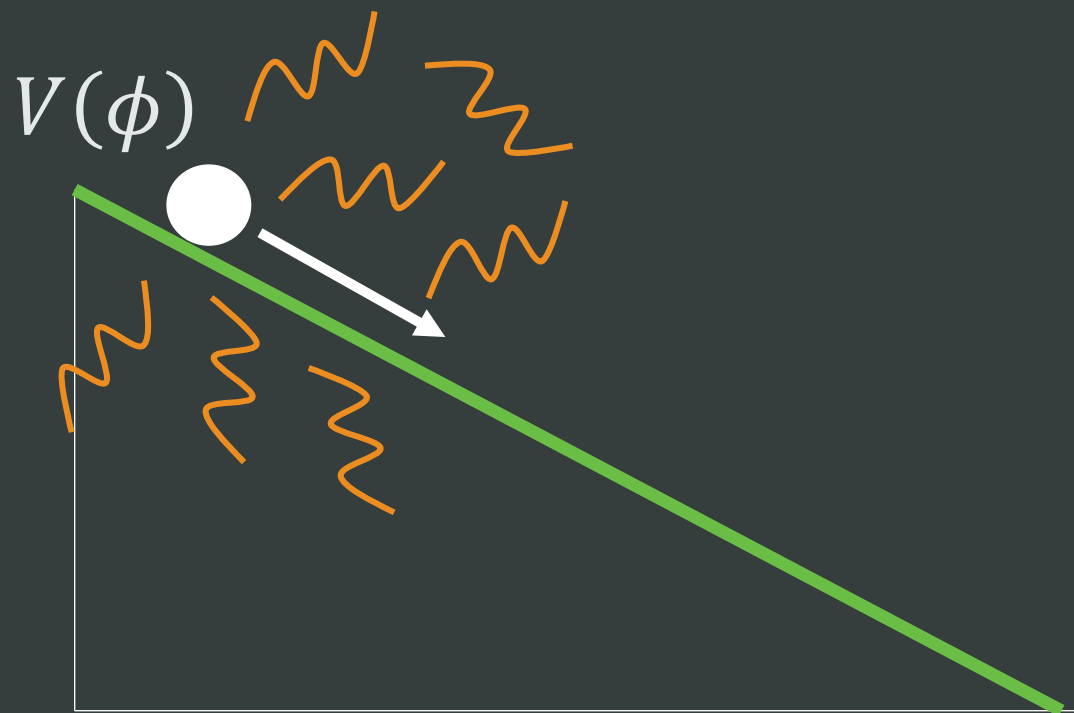
Beyond EDE

Dissipative axion as late dark energy

Scalar coupled to DR **additionally**
experiences **thermal friction**

$$\ddot{\phi} + (3H + \Upsilon) \dot{\phi} + V_{\phi} = 0$$

$$\dot{\rho}_{dr} = -4H\rho_{dr} + \Upsilon\dot{\phi}^2$$



Berghaus, [Karwal](#) et al [2311.08638]

Beyond EDE

Dark energy radiation

Current data:

Planck CMB + BAO + Pantheon SNe

$$V(\phi) = C\phi$$

$$\Omega_{DER} \simeq 0.03 \text{ at } 2\sigma$$

$$100 \times \Lambda\text{CDM radiation } \Omega_\gamma \sim 10^{-4}$$

$$5000 \times \Delta N_{eff} \text{ radiation } \Omega_{N_{eff}} \sim 10^{-5}$$

Future data:

SO CMB + BAO + Roman SNe

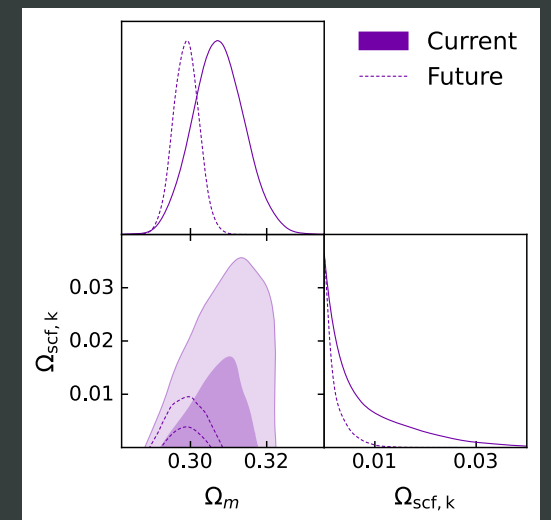
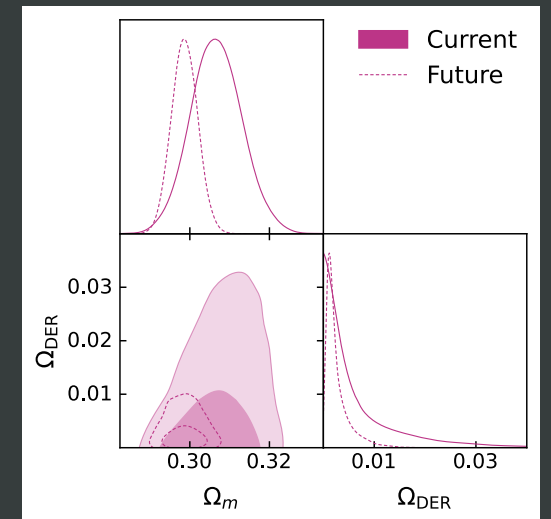
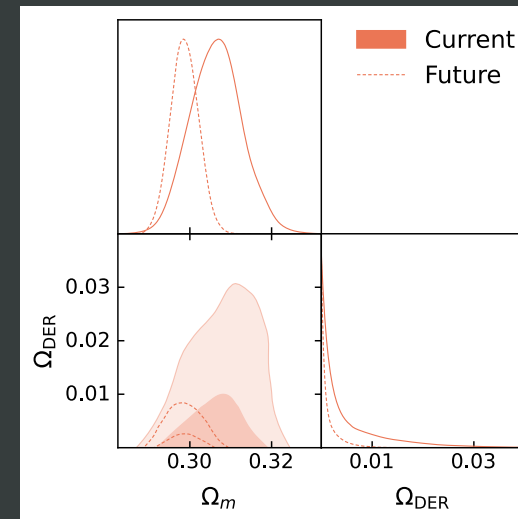
$$\Omega_{DER} \simeq 1\% \text{ at } 2\sigma$$

Recent DESI data:

CMB + DESI + Pan+

$$\Omega_{DER} \simeq 0.03 \text{ at } 1\sigma \text{ with}$$

Berghaus et al [2404.14341]



Minimal DER

$$\Upsilon \propto \rho_{DER}^{3/4}$$

Toy DER

$$\Upsilon = \text{constant}$$

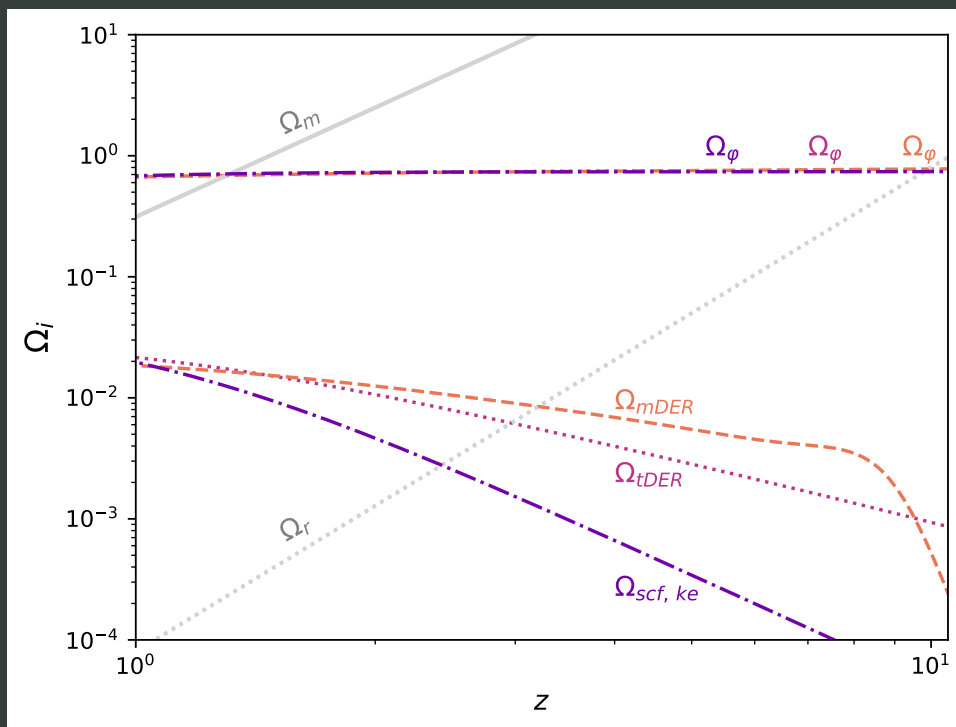
Quintessence

$$\Upsilon = 0$$

Beyond EDE

Dark energy radiation

Λ CDM
 Minimal DER
 Toy DER
 Quintessence



DER produced dynamically in the late universe evades early-universe DR bounds where $\Omega_{DER} \simeq 0$

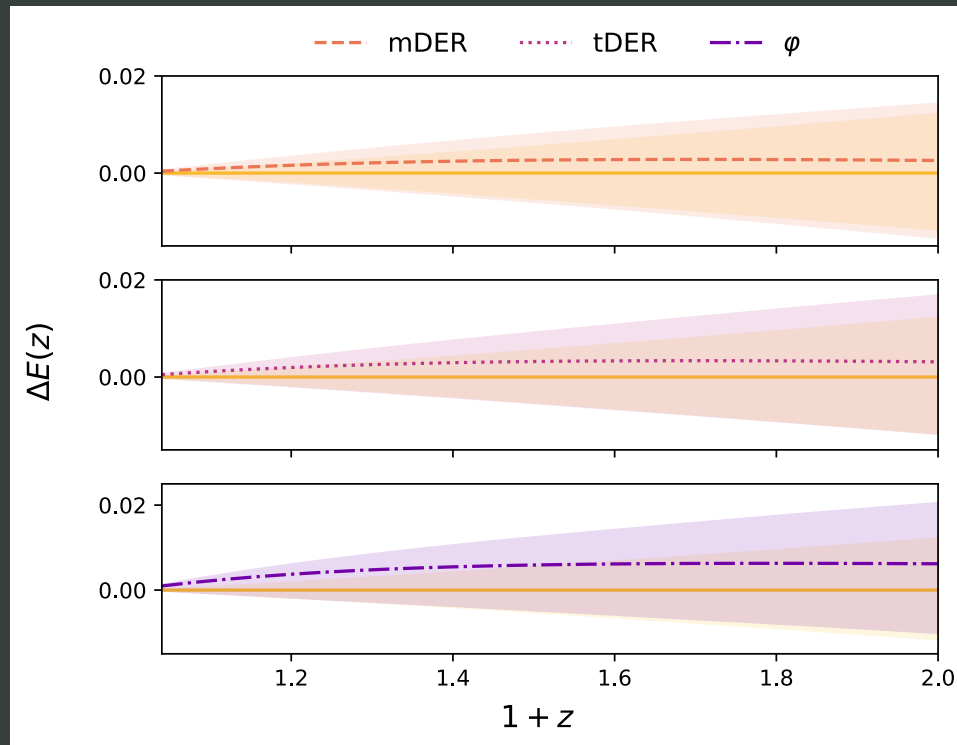
Constraints are dominated by the impact of DER on the background expansion $H(z) = H_0 E(z)$

Berghaus, Karwal et al [2311.08638]

Beyond EDE

Dark energy radiation

Λ CDM
Minimal DER
Toy DER
Quintessence



Berghaus, [Karwal](#) et al [2311.08638]

Neither current or future CMB and SNe data will be able to distinguish these models in

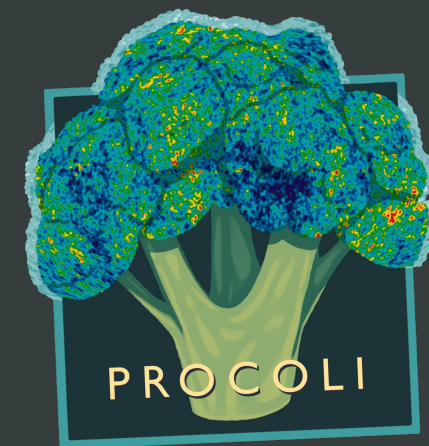
$$E(z) = \frac{H(z)}{H_0}$$

or

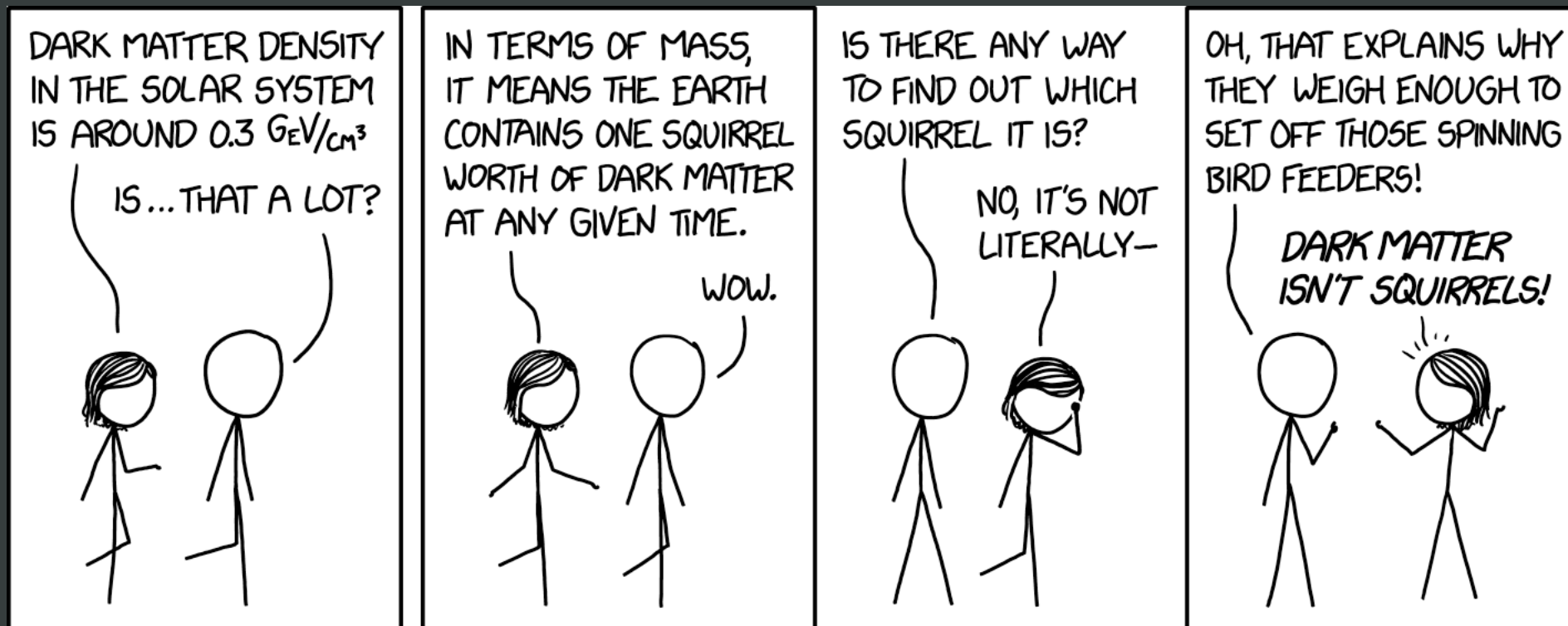
$$w(z)$$

Cosmic tensions, solutions and extensions

- Are the tensions real (CMB lensing sees no S_8 tension)? Do they point to new, undiscovered physics?
- Hubble tension requires a modification to the background universe, at early times
- Early dark energy can resolve the Hubble tension
 - Several fundamental models can form EDE, with details of the model dictating resolution of tension and fit to data
 - Current and future CMB data can detect and to some extent distinguish models
- Challenges to EDE include **the WL tension, a new coincidence problem, improving the fundamental model, prior volume effects**
 - **Model-building insight, using EDE avatars as a stepping stone** – eg. interactions with **dark matter, late dark energy or dark radiation**
 - **Profile likelihoods provide more insight into these models.**
- Models are applicable to other eras of accelerated expansion – **dark energy (DER)** and inflation (See warm inflation papers by Berghaus)
 - Dark radiation dynamically produced in the late universe evades cosmic bounds on ever-present DR. Can be as large as $\Omega_{DER} \simeq 0.03 = 100 \times \Omega_{rad}^{\Lambda CDM}$, with a temperature much higher than that of the CMB
- Inelegance: two independent solutions required for H_0 and WL?
 - H_0 depends on background expansion
 - WL S_8 depends on perturbation evolution



Lets get creative with dark sector physics!



XKCD: 2186