

Tests of Lorentz and CPT Symmetry

outline

1. Introduction
2. Searches of Lorentz Violation
3. Searches of CPT Violation
4. Tests of quantum mechanics
5. Conclusion

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Water Cherenkov Experiments for Precision Physics,
Jagiellonian University, Kraków, Poland, Sep. 18, 2025



Introduction

Lorentz violation

Quantum field theory and general relativity are the foundation of modern physics.

Special relativity is a basis for both quantum field theory and general relativity.

Special relativity is based on Lorentz symmetry

If the universe has a special direction, space doesn't have Lorentz symmetry and Lorentz transformation is violated → Lorentz violation

All fundamental physics phenomena must be experimentally tested including Lorentz symmetry

Modern Physics



Quantum Field Theory

General Relativity

Jadwiga,
"King" of Poland

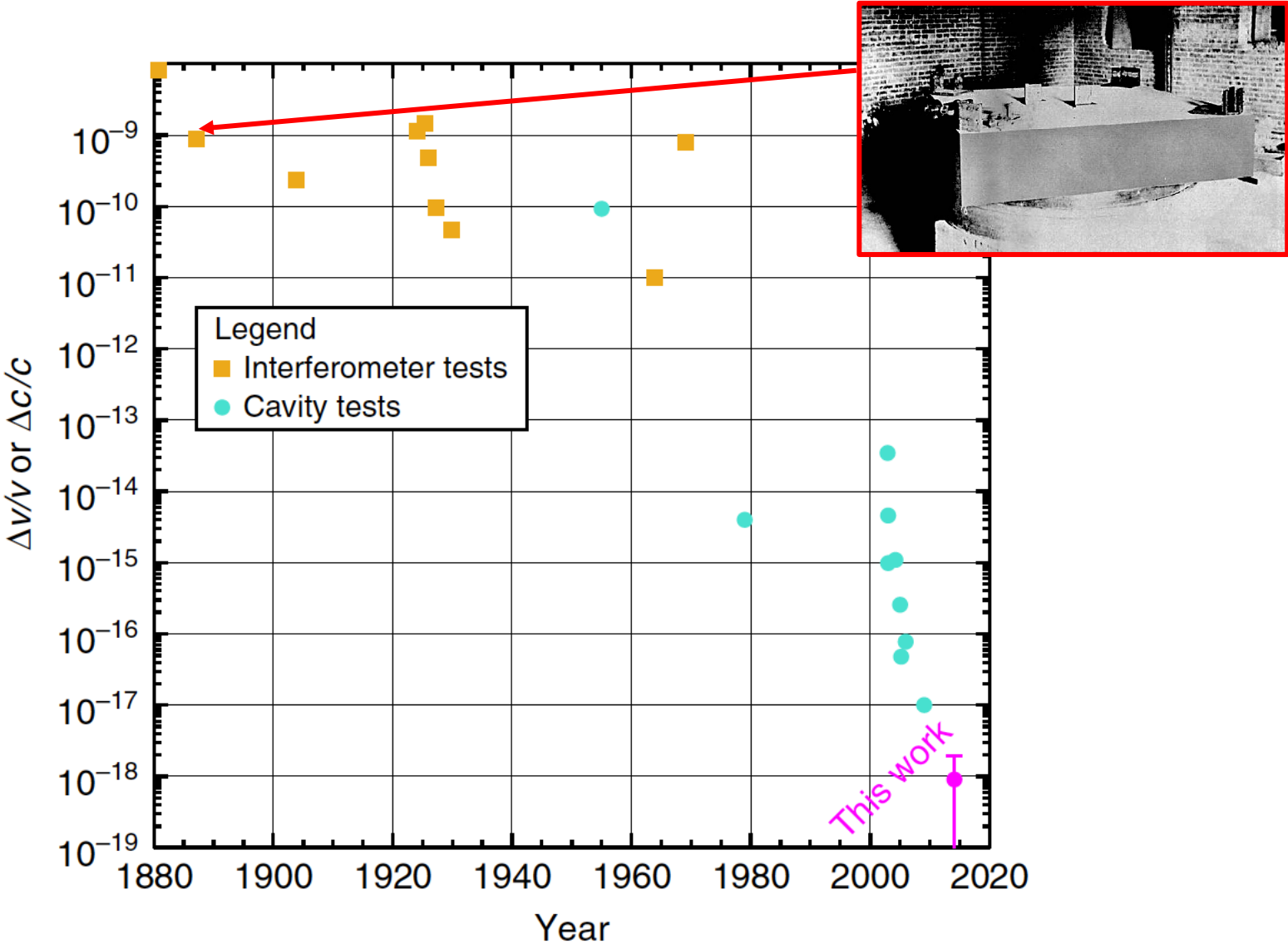
Władysław II
Jagiełło

Lorentz symmetry

Searches of Lorentz violation

Lorentz symmetry is valid down to $\Delta c/c < 10^{-9}$

The experiment has been improved over 100 years.



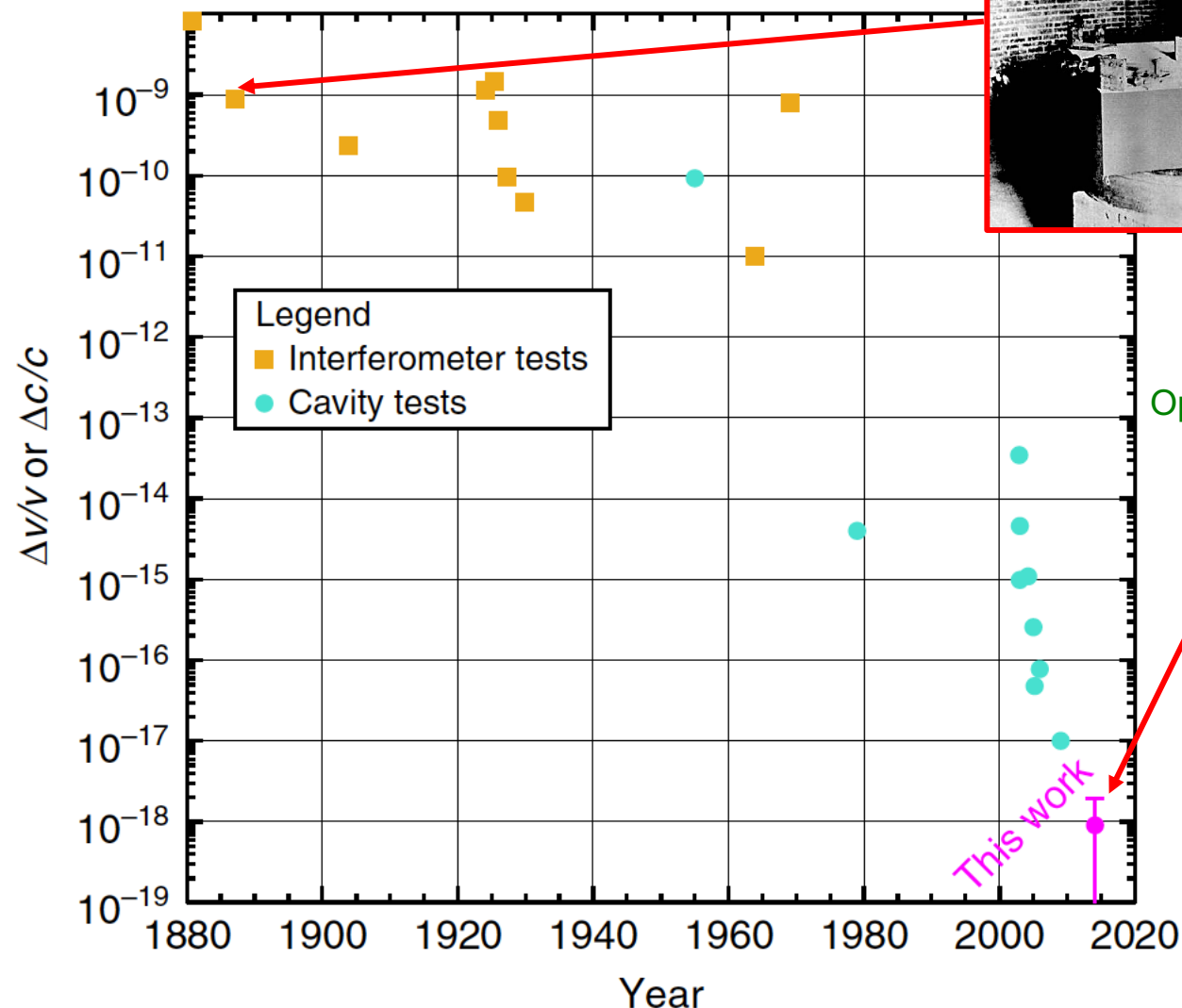
Searches of Lorentz violation

Lorentz symmetry is valid
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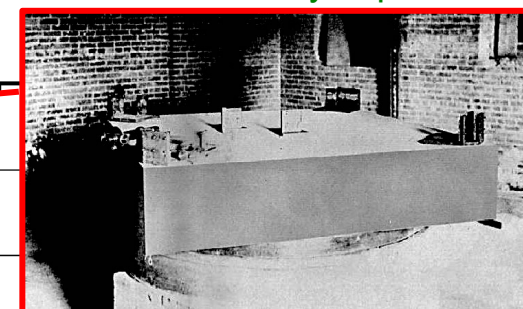
The experiment has been
improved over 100 years.

Technology shift
(interferometer $\rightarrow$ optical
cavity) and $\Delta c/c < 10^{-18}$
(1 billion higher precision
than M-M experiment)

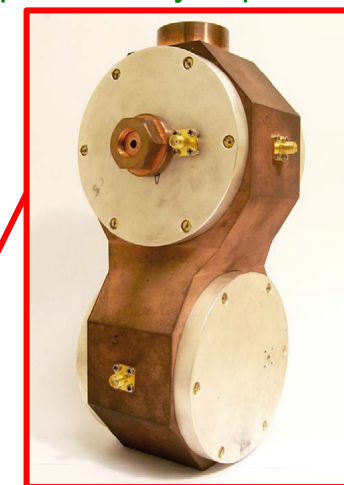
Why we keep testing this?



Michelson-Morley experiment



Optical cavity experiment



Quantum gravity

Searching Lorentz violation is well motivated

Lorentz violation in Planck scale theories

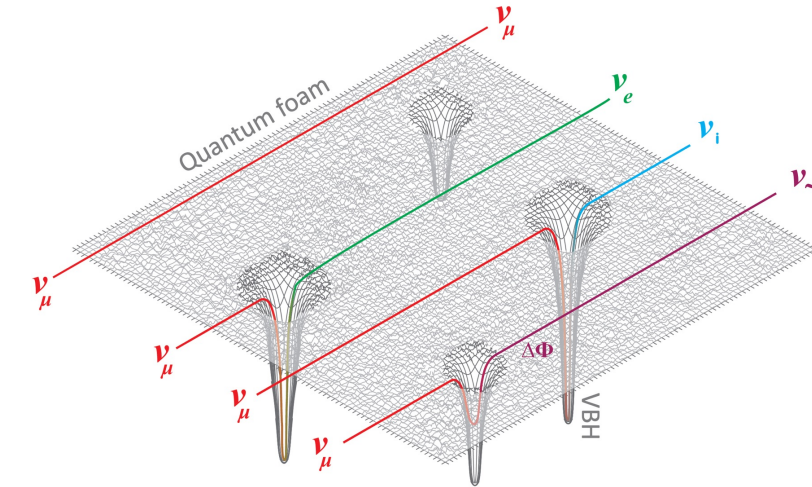
- string theory
- noncommutative field theory
- quantum loop gravity

etc

Lorentz violation is seen as

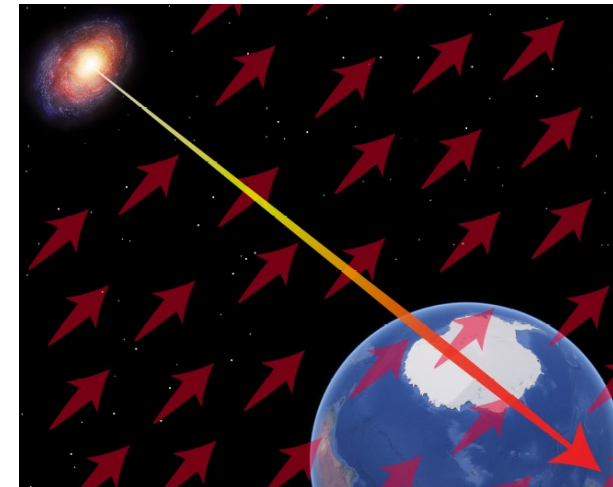
- background field in vacuum (SME)
- spacetime fluctuation (quantum mechanics)

etc



Quantum foam

- quantum fluctuation of space-time



Standard Model Extension (SME)

- parameterize interactions with background field of the universe (æther)

Fundamental Symmetry tests with Neutrinos

Atmospheric neutrinos

- Oscillation length $L \sim 12700$ km (at ~ 35 GeV)
→ the longest interferometer on earth

cf.) LIGO

- 4km arm + mirror ~ 1000 km equivalent

Astrophysical neutrinos

- energy reaches $\sim \text{PeV}$
→ new physics sensitivity $\sim 10^{-26}$ GeV

cf) High precision hydrogen 1S-2S transition

Fractional frequency uncertainty $\sim 4 \times 10^{-15}$

- new physics sensitivity $\sim 10^{-23}$ GeV

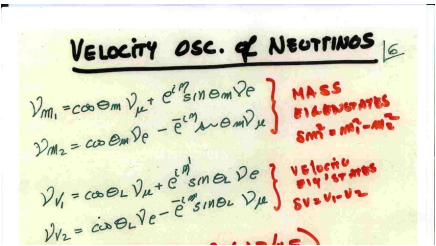
Neutrinos are the best probes
of fundamental symmetry tests!



Searches of Lorentz violation

Lorentz violating neutrino oscillations

One of solutions of neutrino anomaly Glashow's talk, Neutrino 98



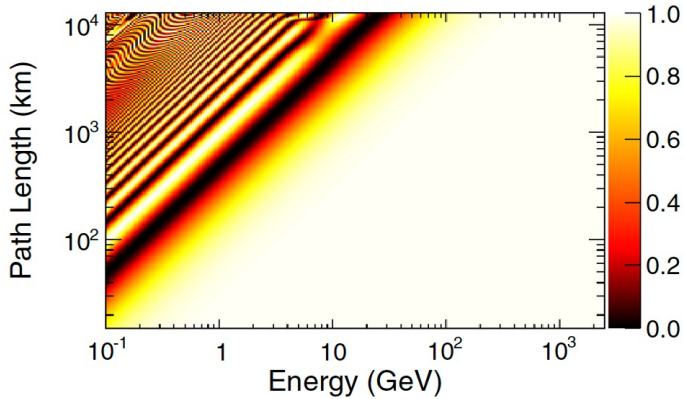
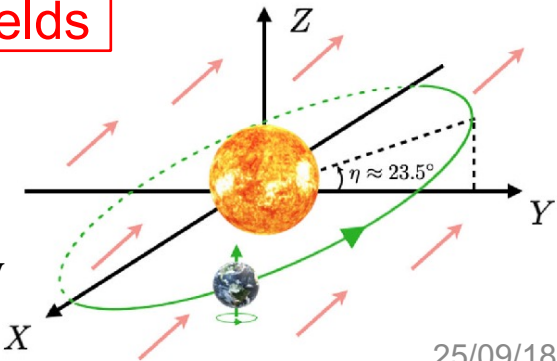
Lorentz violating neutrino oscillation depend on L or LE, not L/E
→ Lorentz violation is small effect, if exists

Lorentz violating neutrino oscillations can be fully parameterized by the Standard-Model Extension (SME) Lagrangian
e.g.) SME Lagrangian for fermion

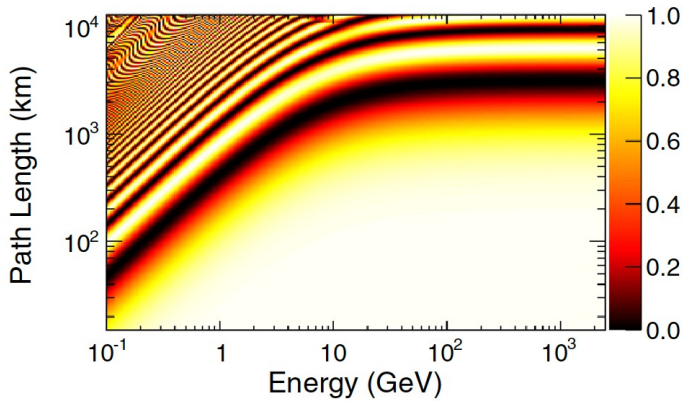
$$\mathcal{L} = i\bar{\psi}\gamma_\mu\partial^\mu\psi - m\bar{\psi}\psi + \underbrace{i\bar{\psi}\gamma_\mu a^\mu\psi}_{\text{Standard Model}} + \underbrace{\bar{\psi}\gamma_\mu c^{\mu\nu}\psi}_{\text{couplings with background fields}} \dots$$

- Physics of Lorentz violation
- Spectrum distortion,
 - Sidereal time dependence

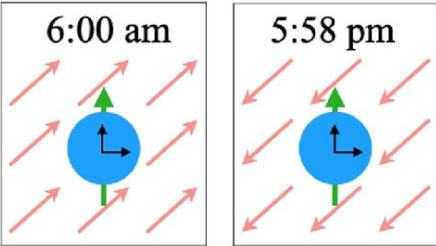
24h 00min 00sec: Solar day
23h 56min 4.1sec: Sidereal day



(a) $\nu_\mu \rightarrow \nu_\mu$, No Lorentz violation



(b) $\nu_\mu \rightarrow \nu_\mu$, $a_{\mu\tau}^T = 10^{-22}$ GeV



Lorentz violation tests with neutrinos – Summary

Limits of all SME parameters are summarized in tables [ArXiv:0801.0287v17](https://arxiv.org/abs/0801.0287v17)

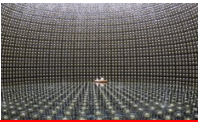
So far, there is no compelling evidence of Lorentz violation

When do we find it???

28-page limits in neutrino sector LV...

Table D31. Neutrino sector, $d = 3$ (part 4 of 6)			
Combination	Result	System	Ref.
$G_{\mu\mu}$	$(-0.3 \pm 3.0) \times 10^{-30}$ GeV	T2K	[260]
$(A_{\mu\mu})_{\text{SM}}$	$(0.4 \pm 3.2) \times 10^{-30}$ GeV	"	[260]
$(A_{\mu\mu})_{\text{NSM}}$	$(0.4 \pm 3.8) \times 10^{-30}$ GeV	"	[260]
$(B_{\mu\mu})_{\text{SM}}$	$(-1.2 \pm 2.6) \times 10^{-30}$ GeV	"	[260]
$(B_{\mu\mu})_{\text{NSM}}$	$(2.0 \pm 3.1) \times 10^{-30}$ GeV	"	[260]
$ C_{\mu\mu} ^2$	$(10.7 \pm 2.6 \pm 1.3) \times (10^{-19} \text{ GeV})^2$	LSND	[261]
$ C_{\mu\mu} ^2 + \frac{1}{2}[(A_{\mu\mu})_{\text{SM}}^2 + \frac{1}{2}(B_{\mu\mu})_{\text{SM}}^2]$	$(9.9 \pm 2.3 \pm 1.4) \times (10^{-19} \text{ GeV})^2$	"	[261]
$ C_{\mu\mu} ^2 + \frac{1}{2}[(A_{\mu\mu})_{\text{SM}}^2 + \frac{1}{2}(B_{\mu\mu})_{\text{SM}}^2] + \frac{1}{2}[(B_{\mu\mu})_{\text{NSM}}^2 + \frac{1}{2}(B_{\mu\mu})_{\text{SM}}^2]$	$(10.5 \pm 2.4 \pm 1.4) \times (10^{-19} \text{ GeV})^2$	"	[261]
$ \langle a_{\mu\mu}^{\text{SM}} \rangle ^2$	$< 6.5 \times 10^{-30}$ GeV	SNO	[251]
$ \langle a_{\mu\mu}^{\text{NSM}} \rangle ^2$	$< 2.8 \times 10^{-30}$ GeV	"	[251]
$ \langle b_{\mu\mu}^{\text{SM}} \rangle ^2$	$< 1.5 \times 10^{-30}$ GeV	"	[251]
$ \langle b_{\mu\mu}^{\text{NSM}} \rangle ^2$	$< 1.7 \times 10^{-30}$ GeV	"	[251]
$\langle a_{\mu\mu} \rangle_{\text{SM}}$	$(-5.6 \pm 8.0) \times 10^{-30}$ GeV	Daya Bay	[252]
$\langle a_{\mu\mu} \rangle_{\text{NSM}}$	$(-0.9 \pm 8.0) \times 10^{-30}$ GeV	"	[252]
$\langle b_{\mu\mu} \rangle_{\text{SM}}$	$< 4.1 \times 10^{-30}$ GeV	Super-Kamiokande	[253]
$\langle b_{\mu\mu} \rangle_{\text{NSM}}$	$< 2.8 \times 10^{-30}$ GeV	"	[253]
$ \langle a_{\mu\mu} \rangle_{\text{SM}} , \langle b_{\mu\mu} \rangle_{\text{SM}} $	$< 7.8 \times 10^{-30}$ GeV	Double Chooz	[256]
$ \langle a_{\mu\mu} \rangle_{\text{NSM}} , \langle b_{\mu\mu} \rangle_{\text{NSM}} $	$< 4.4 \times 10^{-30}$ GeV	"	[256]
$ \langle a_{\mu\mu} \rangle_{\text{SM}} , \langle b_{\mu\mu} \rangle_{\text{SM}} $	$< 9.0 \times 10^{-30}$ GeV	"	[256]
$ \langle a_{\mu\mu} \rangle_{\text{NSM}} , \langle b_{\mu\mu} \rangle_{\text{NSM}} $	$< 2.7 \times 10^{-30}$ GeV	"	[256]
$ \langle a_{\mu\mu} \rangle_{\text{SM}} , \langle b_{\mu\mu} \rangle_{\text{NSM}} , \langle a_{\mu\mu} \rangle_{\text{NSM}} , \langle b_{\mu\mu} \rangle_{\text{SM}} $	$< 7.8 \times 10^{-30}$ GeV	"	[256]
$ \langle a_{\mu\mu} \rangle_{\text{SM}} ^2 + 0.30 \langle a_{\mu\mu} \rangle_{\text{SM}}^2 + 0.0042 \langle a_{\mu\mu} \rangle_{\text{SM}}^2 + 0.0042 \langle a_{\mu\mu} \rangle_{\text{SM}}^2$	$< 6.6 \times 10^{-30}$ GeV	"	[258]
$ \langle a_{\mu\mu} \rangle_{\text{SM}} ^2 + 0.30 \langle a_{\mu\mu} \rangle_{\text{SM}}^2 + 0.0042 \langle a_{\mu\mu} \rangle_{\text{SM}}^2 + 0.0042 \langle a_{\mu\mu} \rangle_{\text{SM}}^2$	$< 7.0 \times 10^{-30}$ GeV	"	[258]
$ \langle a_{\mu\mu} \rangle_{\text{SM}} ^2 + 0.30 \langle a_{\mu\mu} \rangle_{\text{SM}}^2 + 0.0042 \langle a_{\mu\mu} \rangle_{\text{SM}}^2 + 0.0042 \langle a_{\mu\mu} \rangle_{\text{SM}}^2$	$< 5.4 \times 10^{-30}$ GeV	"	[258]
$ \langle a_{\mu\mu} \rangle_{\text{SM}} ^2 + 0.30 \langle a_{\mu\mu} \rangle_{\text{SM}}^2 + 0.0042 \langle a_{\mu\mu} \rangle_{\text{SM}}^2 + 0.0042 \langle a_{\mu\mu} \rangle_{\text{SM}}^2$	$< 5.4 \times 10^{-30}$ GeV	"	[258]
$ \langle a_{\mu\mu} \rangle_{\text{SM}} ^2 + 0.30 \langle a_{\mu\mu} \rangle_{\text{SM}}^2 + 0.0042 \langle a_{\mu\mu} \rangle_{\text{SM}}^2 + 0.0042 \langle a_{\mu\mu} \rangle_{\text{SM}}^2$	$< 2 \times 10^{-30}$ GeV	Lepton, SU(2) _L invariance	[239]*
$ \langle a_{\mu\mu} \rangle_{\text{SM}} ^2 + 0.30 \langle a_{\mu\mu} \rangle_{\text{SM}}^2 + 0.0042 \langle a_{\mu\mu} \rangle_{\text{SM}}^2 + 0.0042 \langle a_{\mu\mu} \rangle_{\text{SM}}^2$	$< 4 \times 10^{-30}$ GeV	"	[239]*
$ \langle a_{\mu\mu} \rangle_{\text{SM}} ^2 + 0.30 \langle a_{\mu\mu} \rangle_{\text{SM}}^2 + 0.0042 \langle a_{\mu\mu} \rangle_{\text{SM}}^2 + 0.0042 \langle a_{\mu\mu} \rangle_{\text{SM}}^2$	$< 8.2 \times 10^{-30}$ GeV	SNO	[251]
$ \langle a_{\mu\mu} \rangle_{\text{SM}} ^2 + 0.30 \langle a_{\mu\mu} \rangle_{\text{SM}}^2 + 0.0042 \langle a_{\mu\mu} \rangle_{\text{SM}}^2 + 0.0042 \langle a_{\mu\mu} \rangle_{\text{SM}}^2$	$< 8.4 \times 10^{-30}$ GeV	"	[251]
$ \langle a_{\mu\mu} \rangle_{\text{SM}} ^2 + 0.30 \langle a_{\mu\mu} \rangle_{\text{SM}}^2 + 0.0042 \langle a_{\mu\mu} \rangle_{\text{SM}}^2 + 0.0042 \langle a_{\mu\mu} \rangle_{\text{SM}}^2$	$< 2.9 \times 10^{-30}$ GeV	"	[251]
$ \langle a_{\mu\mu} \rangle_{\text{SM}} ^2 + 0.30 \langle a_{\mu\mu} \rangle_{\text{SM}}^2 + 0.0042 \langle a_{\mu\mu} \rangle_{\text{SM}}^2 + 0.0042 \langle a_{\mu\mu} \rangle_{\text{SM}}^2$	$< 3.2 \times 10^{-30}$ GeV	"	[251]
$\langle a_{\mu\mu} \rangle_{\text{SM}}$	$(9.4 \pm 45) \times 10^{-30}$ GeV	Daya Bay	[252]
$\langle a_{\mu\mu} \rangle_{\text{NSM}}$	$(-9.4 \pm 45) \times 10^{-30}$ GeV	"	[252]
$ \langle a_{\mu\mu} \rangle_{\text{SM}} , \langle a_{\mu\mu} \rangle_{\text{NSM}} $	$< 1.9 \times 10^{-30}$ GeV	Super-Kamiokande	[262]*
$ \langle a_{\mu\mu} \rangle_{\text{SM}} , \langle a_{\mu\mu} \rangle_{\text{NSM}} $	$< 4.8 \times 10^{-30}$ GeV	T2K	[263]
$ \langle a_{\mu\mu} \rangle_{\text{SM}} , \langle a_{\mu\mu} \rangle_{\text{NSM}} $	$< 6.3 \times 10^{-30}$ GeV	Super-Kamiokande	[264]*

Spectral distortion



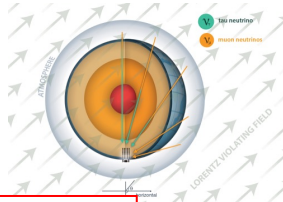
Super-Kamiokande

PRD91(2015)052003



AMANDA

PRD79(2009)102005



IceCube

Nature Physics 14(2018)961



IceCube

Nature Physics, 18(2022)1287

Daya Bay



Daya Bay

PRD98(2018)092013

Sidereal variation



LSND

PRD72(2005)076004



MiniBooNE

PLB718(2013)1303



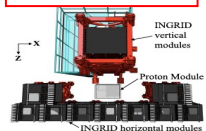
MINOS ND

PRL101(2008)151601



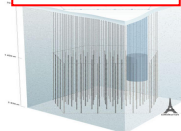
MINOS FD

PRL105(2010)151601



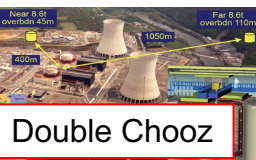
T2K ND

PRD95(2017)111101



IceCube

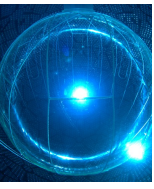
PRD82(2010)112003



Double Chooz

PRD86(2013)112009

SNO



SNO

PRD98(2018)112013

Flavor ratio

Seasonal variation

tkatori@cern.ch

25/09/18

10

KING'S
College
LONDON

When do we find Lorentz violation???

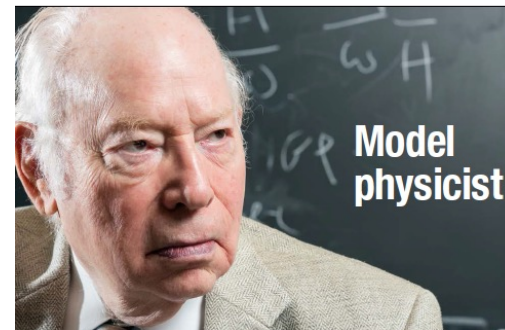
Lorentz violation is motivated by Planck scale theories, so it is suppressed with the power of Planck mass ($\sim 10^{19} \text{ GeV}$). In effective field theory, **non-renormalizable operators** are the signature of new physics, dimension analysis guides target sensitivity to look for Lorentz violation.

$$a^{(5)} \sim \frac{1}{M_{Pl}}, \quad c^{(6)} \sim \left(\frac{1}{M_{Pl}} \right)^2, \quad etc$$

dimension-5 LV operator, $a^{(5)} < 10^{-19} \text{ GeV}^{-1}$

dimension-6 LV operator, $c^{(6)} < 10^{-38} \text{ GeV}^{-2}$, etc

These numbers can be used as a guidance to design new experiments. **Astrophysical signals** have advantages to look for these operators.



Steven Weinberg
([CERN Courier Nov. 2017](#))

“We don’t know anything about non-renormalizable interaction terms, but I’ll swear they are there!”

Lorentz violation in Astrophysics

Highest energy particles – ultra-high-energy cosmic rays

Longest propagating waves – gravitational waves, cosmic microwave background

High-energy and long propagation – gamma-ray, high-energy neutrinos



Contents lists available at [ScienceDirect](https://www.sciencedirect.com)

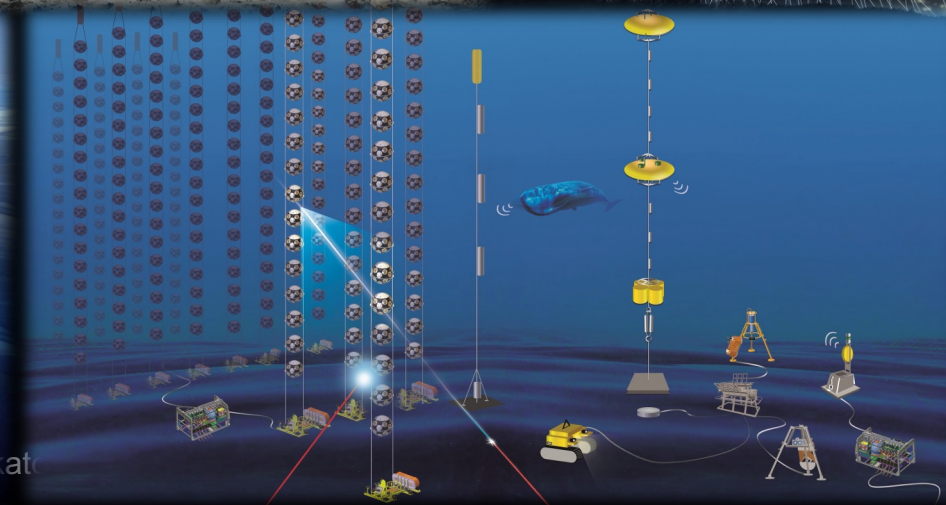
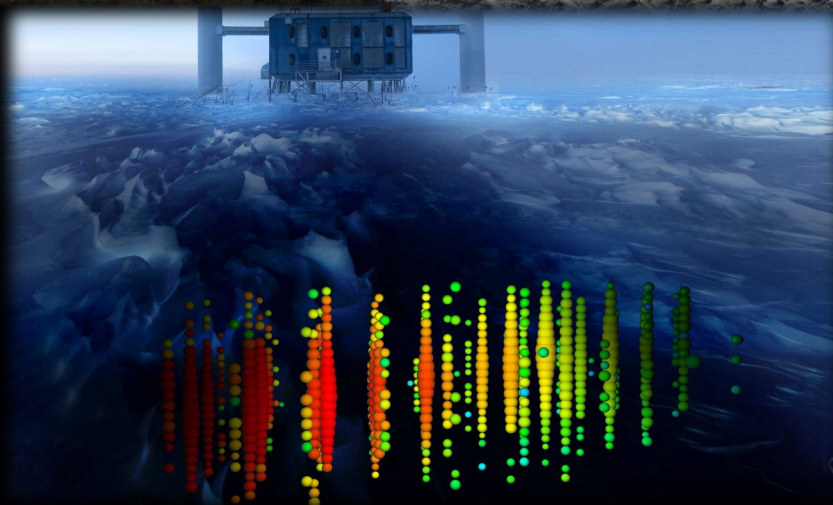
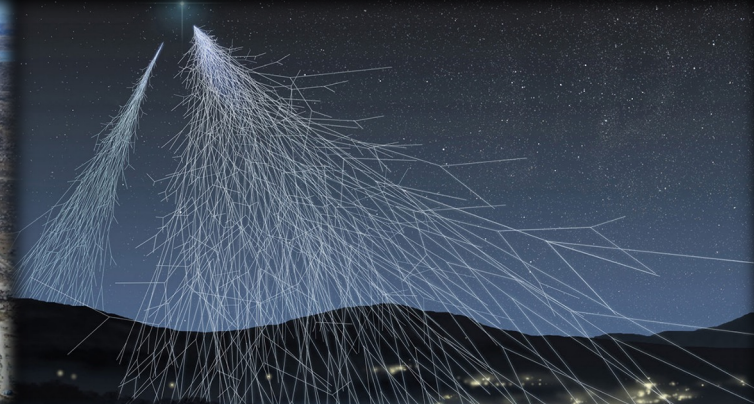
Progress in Particle and Nuclear Physics

journal homepage: www.elsevier.com/locate/ppnp



Review

Quantum gravity phenomenology at the dawn of the multi-messenger era—A review

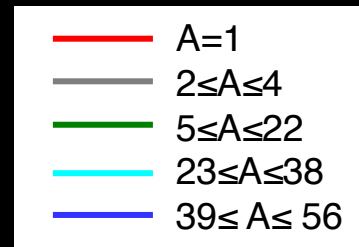
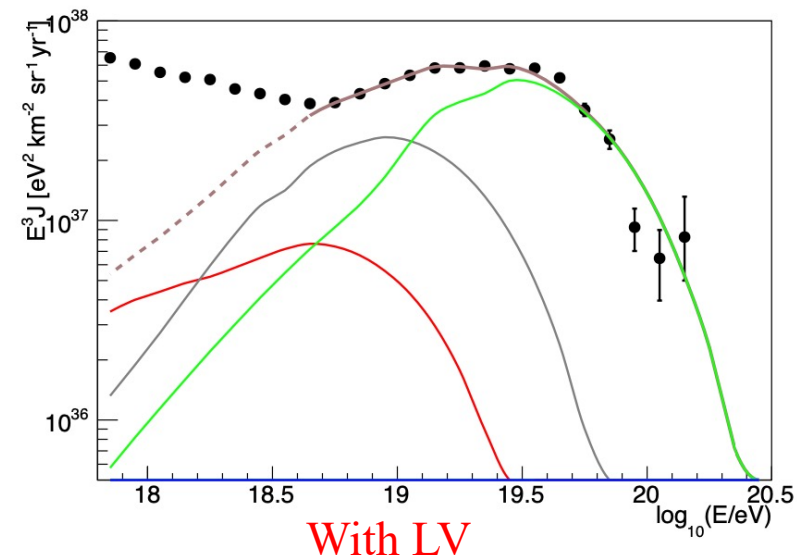
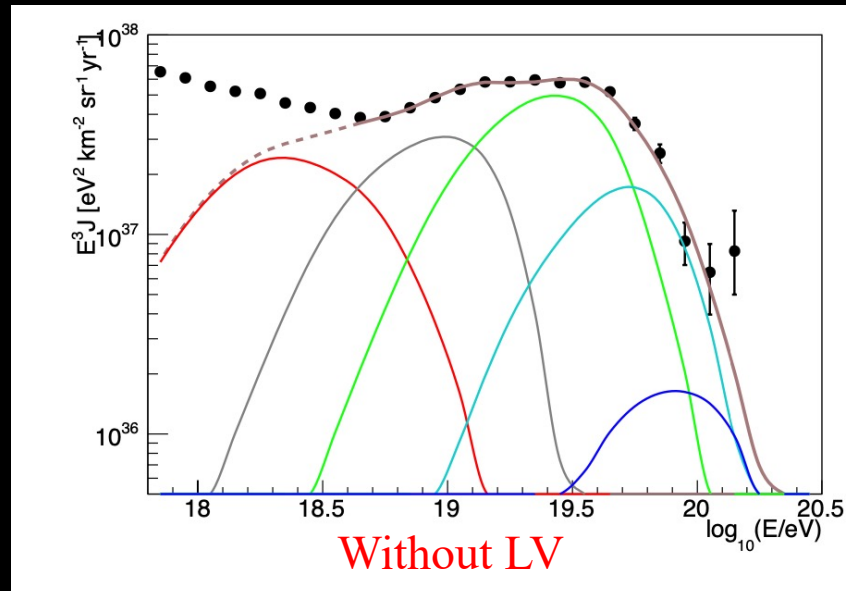
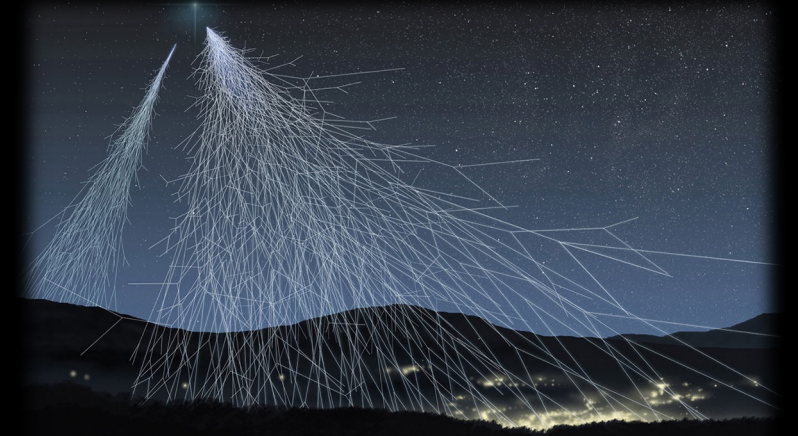


Cut-off in high-energy cosmic ray spectrum

Lorentz violation = media in vacuum

- Attenuate high-energy cosmic rays

$$E^2 = p^2 + m^2 + a^{(5)}E^3 + c^{(6)}E^4 + \dots$$



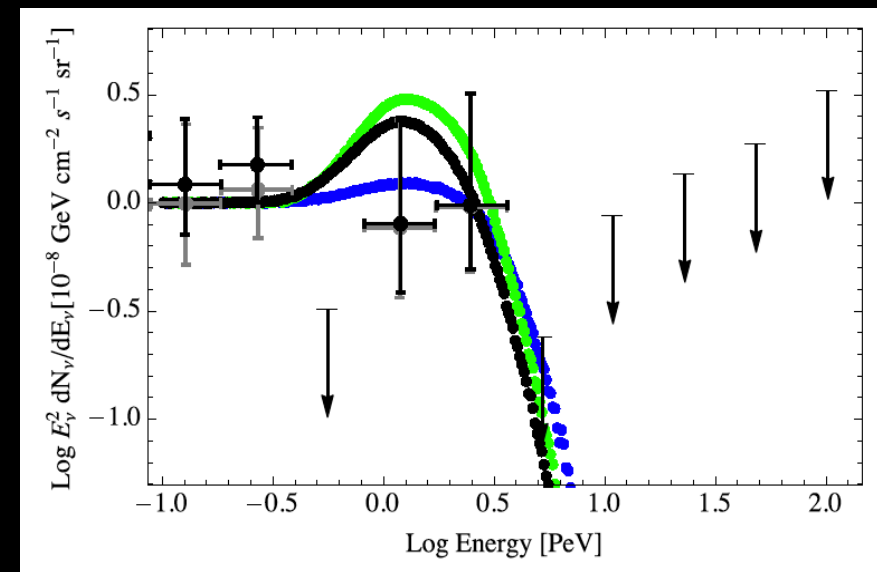
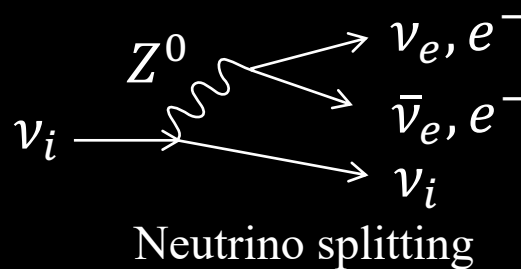
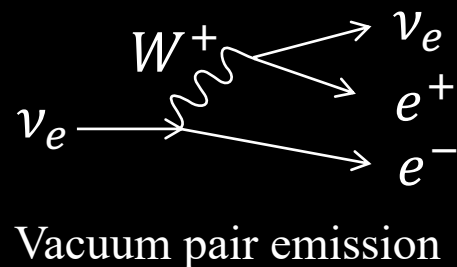
Auger UHECR spectrum

Cut-off in high-energy cosmic ray spectrum

Lorentz violation = media in vacuum

- Attenuate high-energy cosmic rays

$$E^2 = p^2 + m^2 + a^{(5)}E^3 + c^{(6)}E^4 + \dots$$



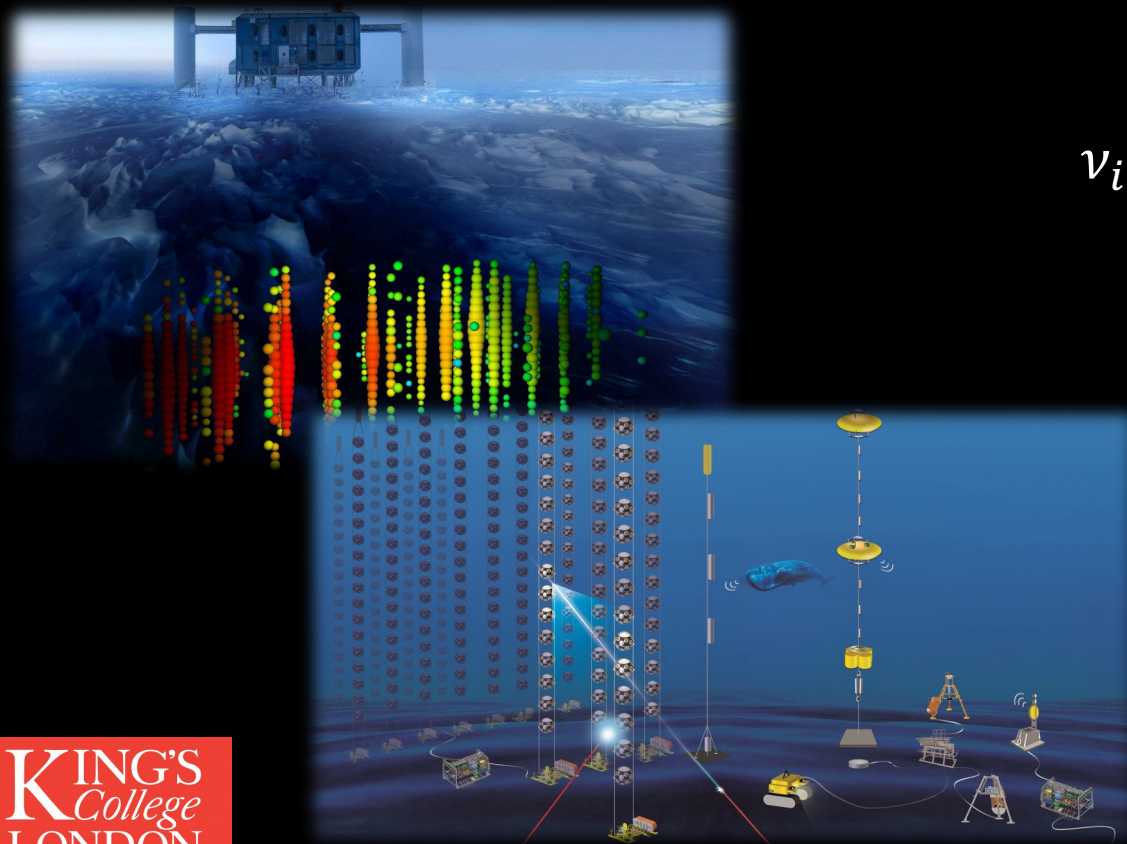
IceCube neutrino spectrum distortion

Lorentz violating field cause radiation in vacuum

- High-energy neutrinos are attenuated

- KM3NeT 220 PeV neutrino (KM3-230213A)

$$\delta \equiv c_v^2 - 1 < 4 \times 10^{-22}$$



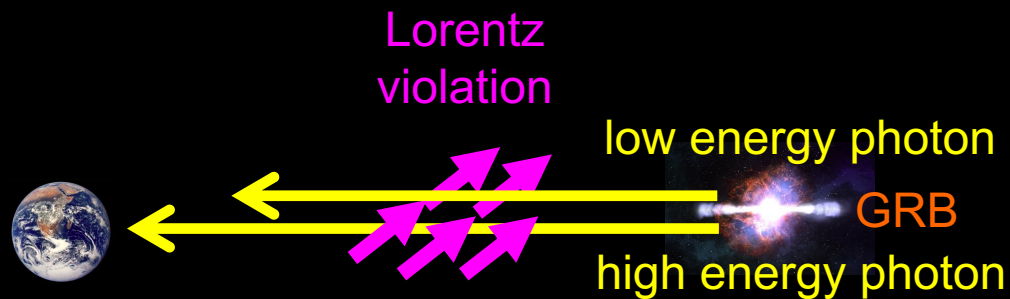
Time-of-flight of high-energy cosmic rays

Lorentz violation = media in vacuum
 - Anomalous time dependent effects

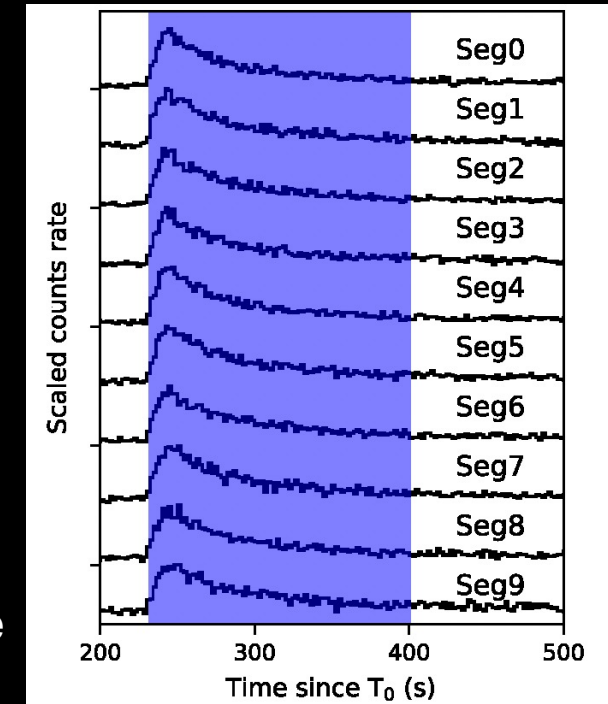
Gamma Ray Bursts

- Energy dependent light curve distortion

$$\delta v \sim E k_{00}^{(5)} + E^2 c_{00}^{(6)} + \dots$$



LHASSO energy-
dependent light curve
of GRB221009A

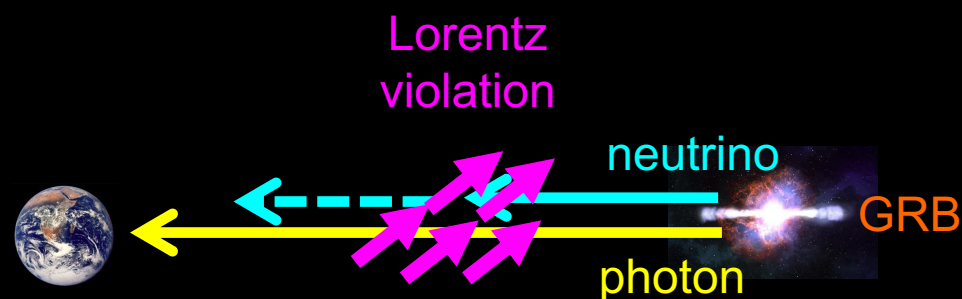


Time-of-flight of high-energy cosmic rays

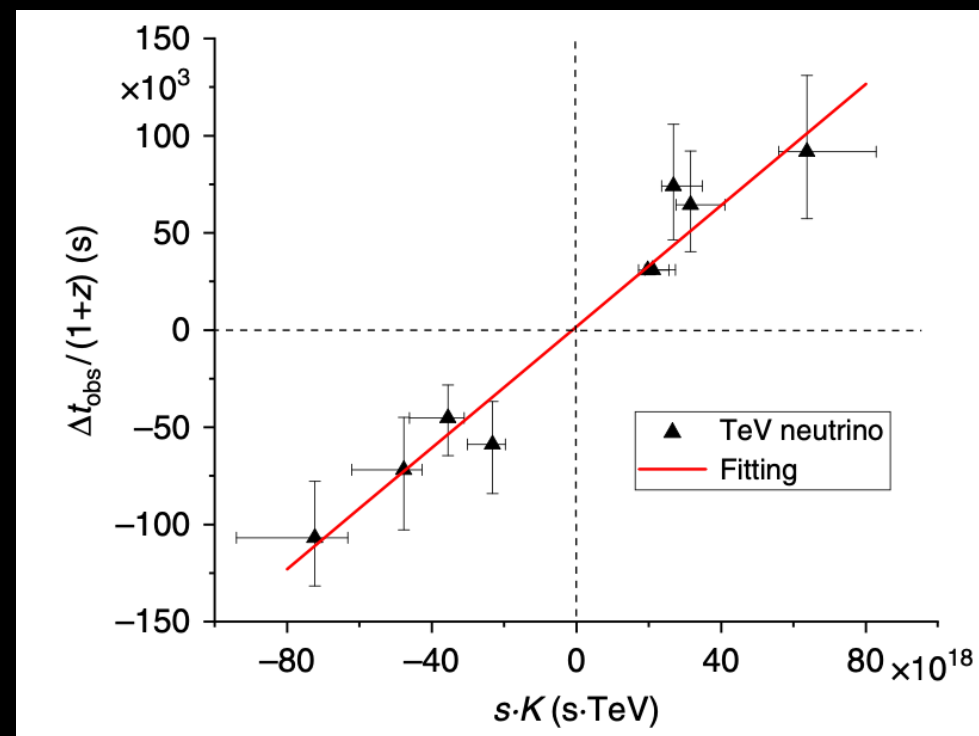
Lorentz violation = media in vacuum
- Anomalous time dependent effects

Gamma Ray Bursts

- Energy dependent light curve distortion
- Neutrino time-of-flight ($a^{(5)}$ =CPT odd)
 $\delta v \sim E a^{(5)} + E^2 c^{(6)} + \dots$



CPT odd Lorentz violation: $a^{(5)} \overset{\nu \leftrightarrow \bar{\nu}}{\longleftrightarrow} -a^{(5)}$



IceCube-GRB coincidence candidates with Lorentz violation

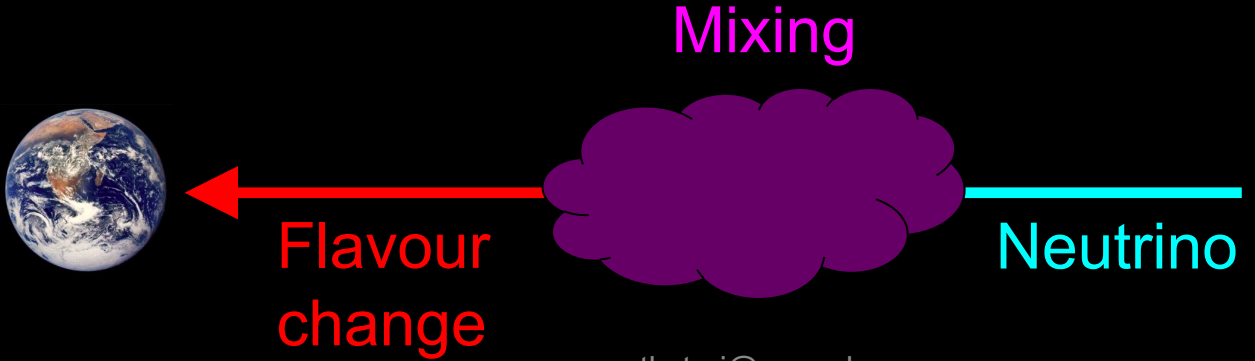
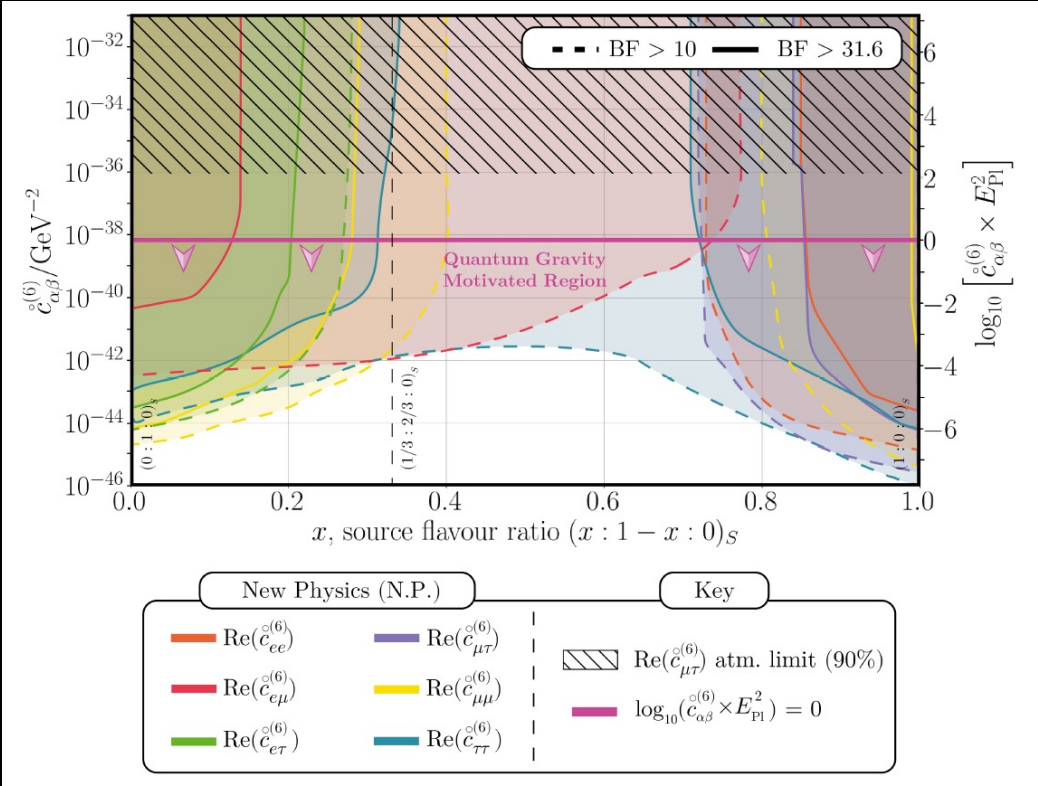
Anomalous neutrino flavour mixing

Lorentz violation = media in vacuum
- MSW-like effect in vacuum

Neutrino mixings are macroscopic quantum effects and sensitive to small effects.

Sensitive to the target region of Quantum Gravity
($< 1/M_{Pl}^2 \sim 10^{-38} GeV^{-2}$ for dim-6 operators)

IceCube Lorentz violation search through astrophysical neutrino flavour



Future of high-energy neutrino astronomy

Higher energy gives better sensitivity to new physics?

Effective area of neutrino telescopes is limited
Cherenkov neutrino telescopes

Future technologies;

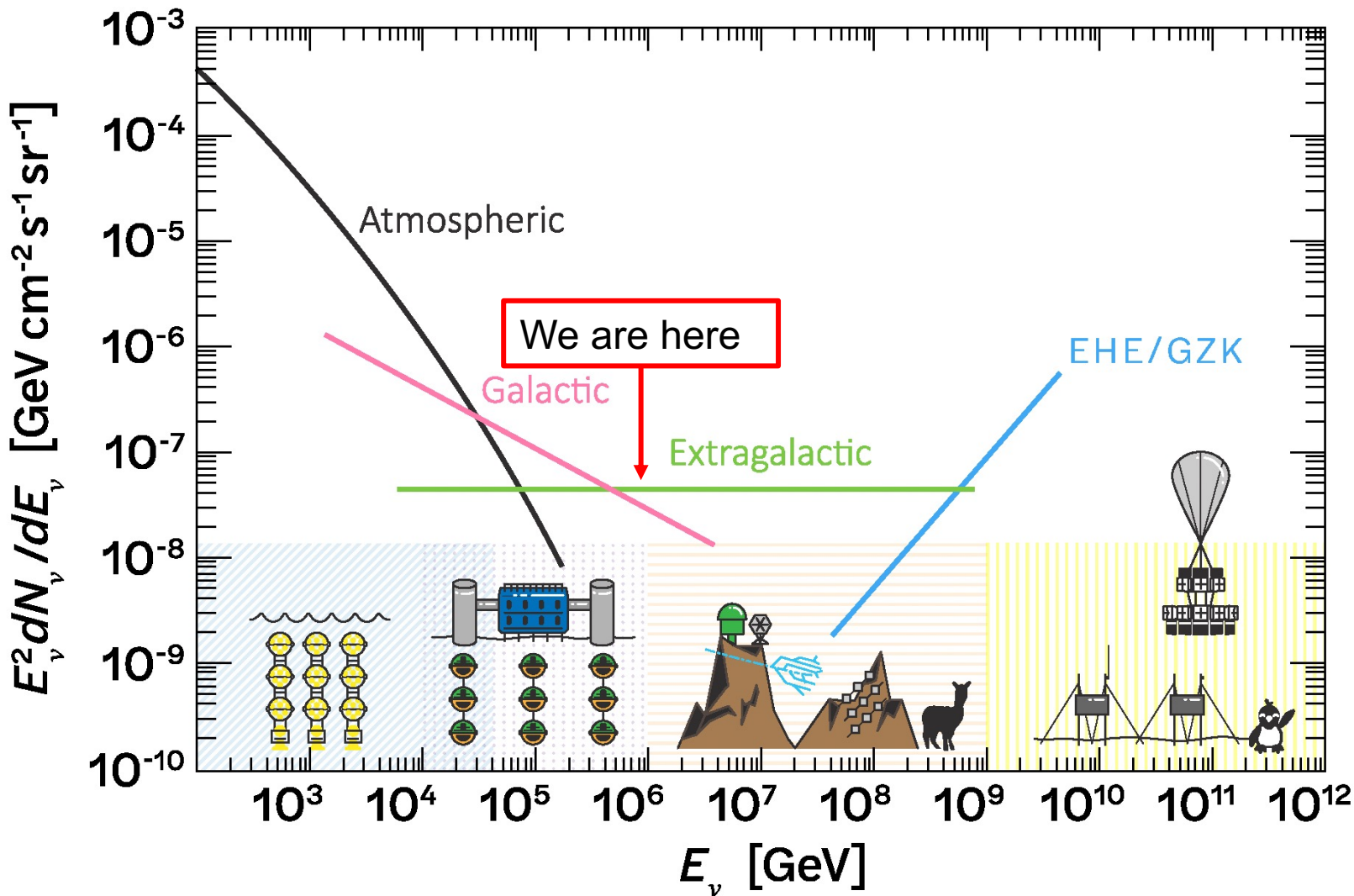
- Radio telescope

PUEO, ARIANNA, RNO-G, IceCube-Gen2, TAROGE-M, Beacon, GRAND

- Air shower

Trinity, POEMMA, TAMBO, Auger/GCOS

etc



Searches of CPT violation

Test of Direct CPT violation

Direct CPT violation

- Comparisons of particles and anti-particles
- $|\Delta m_{21}^2 - \Delta \bar{m}_{21}^2| < 5.9 \times 10^{-5} \text{ eV}^2$
- $|\Delta m_{31}^2 - \Delta \bar{m}_{31}^2| < 0.8 - 1.1 \times 10^{-3} \text{ eV}^2$

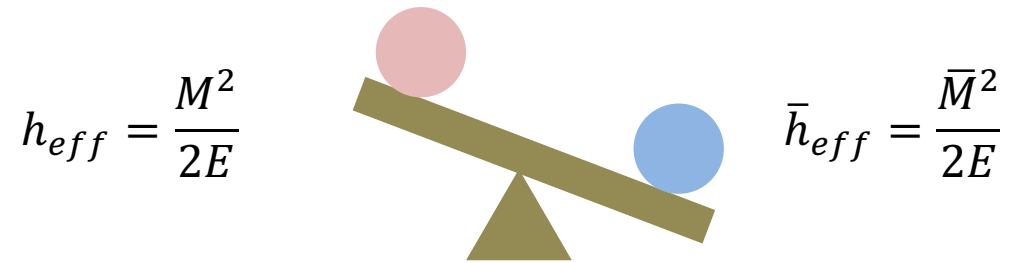
cf.) Kaon system

- $|m(K^0) - m(\bar{K}^0)|/m(K^0) < 6 \times 10^{-19} \text{ GeV}$
- $\rightarrow |m^2(K^0) - m^2(\bar{K}^0)| < 0.25 \text{ eV}^2$

cf.) Hydrogen-Antihydrogen charge/mass ratio (BASE) [BASE, Nature 601\(2022\) 53](#)

- $r_H < 2 \times 10^{-27} \text{ GeV}$

Neutrinos oscillation experiments provide the most precise direct CPT violation tests for elementary particles (Hyper-Kamiokande, JUNO, DUNE, etc)



Test of General CPT violation

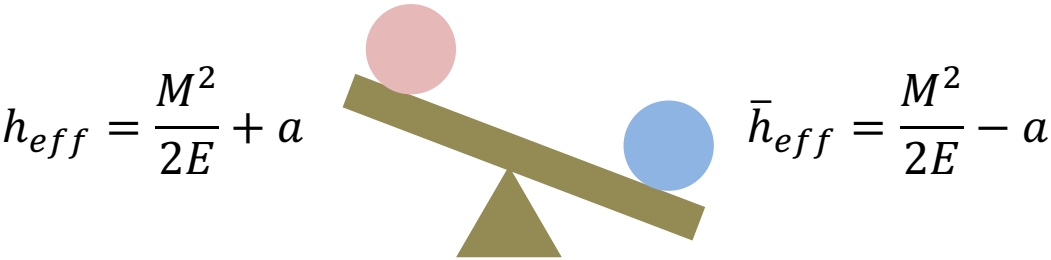
Lorentz and CPT violation

- Interactive local QFT
- CPT odd SME parameters ($a \overset{\nu \leftrightarrow \bar{\nu}}{\longleftrightarrow} -a$)
- High-precision LV test = High-precision CPT test

CPT violation with Lorentz invariant

- Non-local interaction
- Theoretical challenges

Particle-Antiparticle comparison remain an important test of CPT violation



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CPT Violation Implies Violation of Lorentz Invariance

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(Received 28 January 2002; published 18 November 2002)

A interacting theory that violates *CPT* invariance necessarily violates Lorentz invariance. On the other hand, *CPT* invariance is not sufficient for out-of-cone Lorentz invariance. Theories that violate *CPT* by having different particle and antiparticle masses must be nonlocal.



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CPT violation does not lead to violation of Lorentz invariance and vice versa

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Particle – Antiparticle comparison

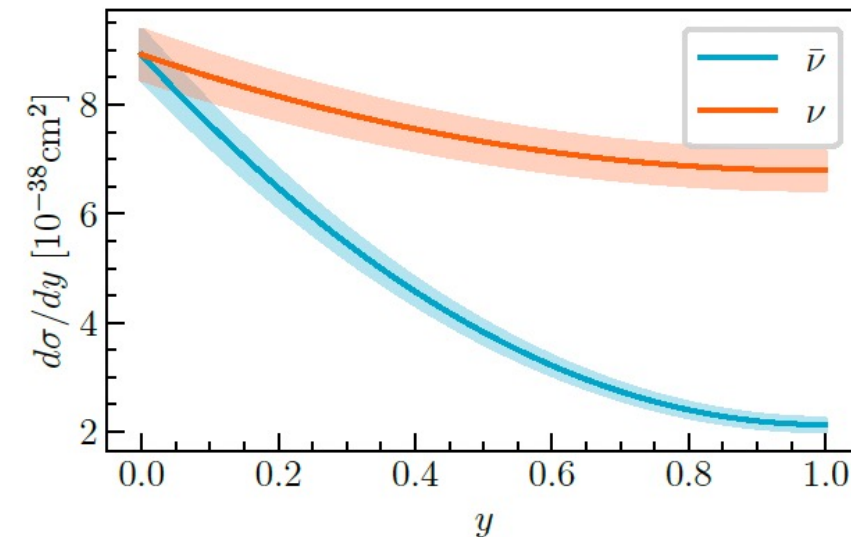
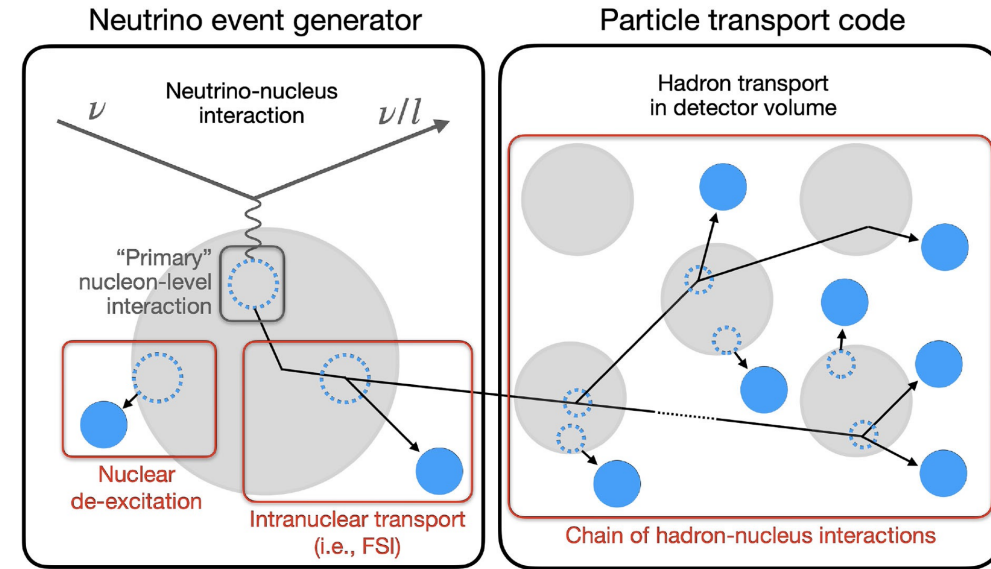
In general, charge separation of neutrinos are not easy for water Cherenkov detector

Low energy – Michel electron and nucleon multiplicity

- $\nu_\mu + n \rightarrow \mu^- + p$ vs. $\bar{\nu}_\mu + p \rightarrow \mu^+ + n$
- $\nu_\mu + p \rightarrow \mu^- + \Delta^{++}$ vs. $\bar{\nu}_\mu + p \rightarrow \mu^+ + \Delta^0$
- Timing, proton and neutron tagging
- Good nuclear physics for precise simulation

Medium energy – Inelasticity

- $\nu + X \rightarrow l + \text{hadrons}, y_{eff} = \frac{E_{had}}{E_{had} + E_{lep}}$
- Key to measure mass hierarchy with atmospheric neutrinos
- Good hadron physics for precise simulation



DIS inelasticity distribution

Tests of Quantum Mechanics

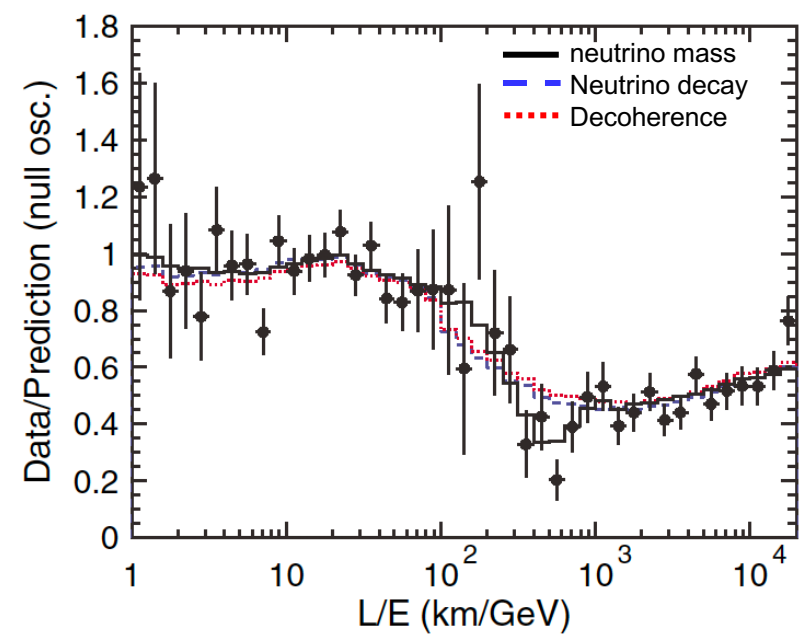
Test of Quantum Mechanics

Quantum decoherence

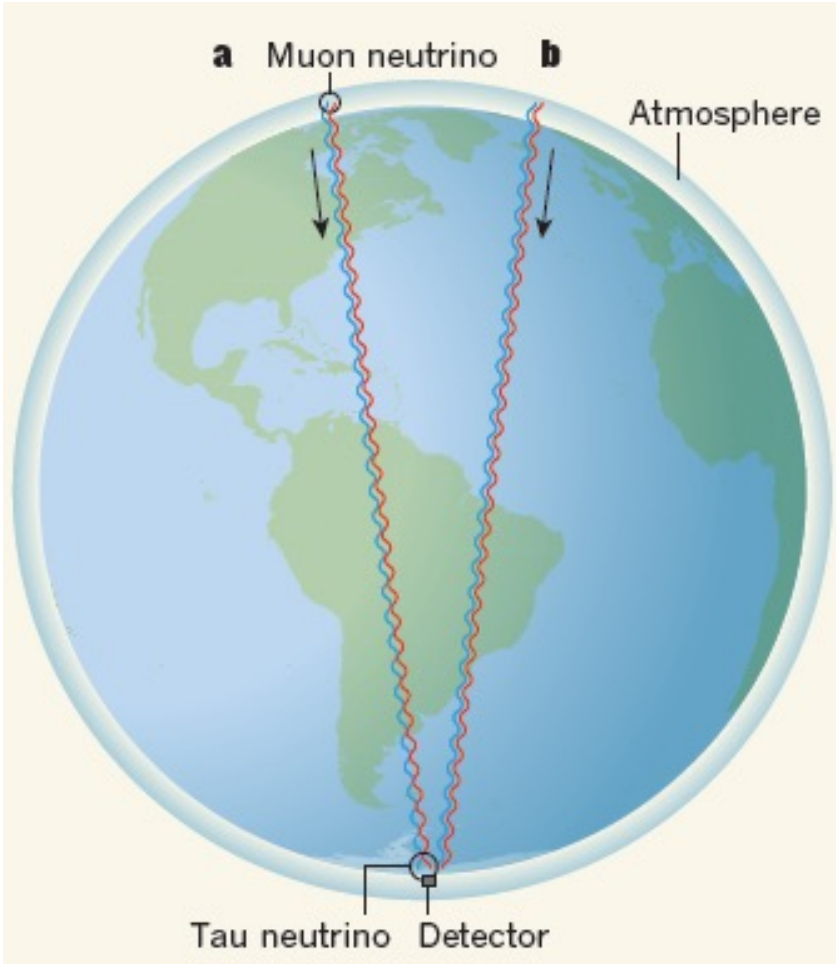
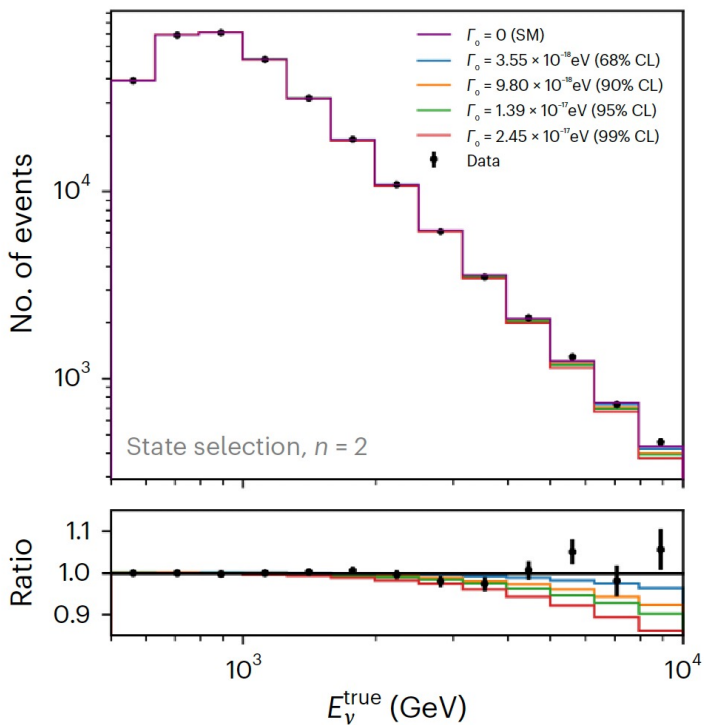
- One of solutions of neutrino anomaly
- Quantum decoherence dumps coherence, no oscillation
- Quantum decoherence is small effect, if exists

[SuperK, PRL93\(2004\)101801](#)

week ending
3 SEPTEMBER 2004



[IceCube, Nature Physics, 20 \(2024\) 913](#)



[IceCube, Nature Physics 14 \(2018\) 961](#)

Test of Quantum Mechanics

Quantum decoherence

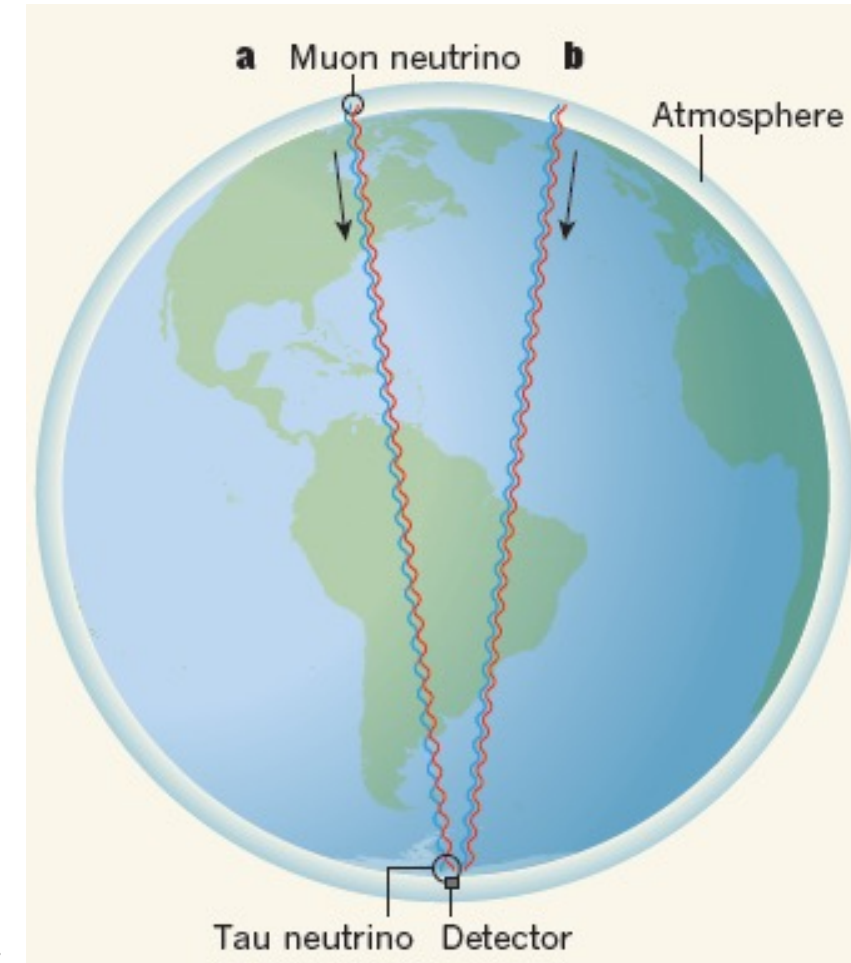
- One of solutions of neutrino anomaly
- Quantum decoherence dumps coherence, no oscillation
- Quantum decoherence is small effect, if exists

Atmospheric neutrino oscillation is the biggest interferometer on Earth to test quantum mechanics

Legget-Garg inequality - Correlation of time sequence

Nambu quantum mechanics - 2-dimensional phase rotation
etc

Active field but not many applications to neutrino physics yet



[IceCube, Nature Physics 14 \(2018\) 961](#)

Conclusion

Lorentz violation is motivated from Planck-scale theories

There is a worldwide effort to look for Lorentz violation, using various state-of-the-art techniques, but so far no compelling evidence of Lorentz violation

Astrophysical sources are powerful tools to look for Lorentz violation

Neutrino oscillations are one of the most precise test of CPT and quantum mechanics

Thank you for your attention!



Backup

Models of Lorentz violation

String theory, [Kostelecký and Samuel, PRD39 \(1989\) 683](#)

Ultra-light dark matter, [Argüelles, Farrag, TK, ArXiv:2404.10926](#)

Quintessence, [Ando, Kamionkowski, and Mocioiu, PRD80 \(2009\) 123522](#)

Loop quantum gravity, [Gambini and Pullin, PRD59 \(1999\) 124021](#)

Non-commutative field theory, [Carroll, Harvey, Kostelecký, Lane, Okamoto, PRL87 \(2001\) 141601](#)

Hořava-Lifshitz gravity, [Pospelov and Shang, PRD85 \(2012\) 105001](#)

Lee-Wick theory, [Myers and Pospelov, PRL90 \(2003\) 211601](#)

Long range force, [Bustamante, Agarwalla, PRL122\(2019\)061103](#)

Torsion, [Kostelecký, Russell, Tasson, PRL100\(2008\)111102](#)

and many more!

Effective Lorentz violation (spontaneous Lorentz symmetry breaking) is compatible with Riemann geometry; however, Intrinsic Lorentz Violation is not

Finsler geometry [Kostelecký and Li, PRD104 \(2021\) 044054](#) got lots of attention recently, to go beyond Riemann geometry

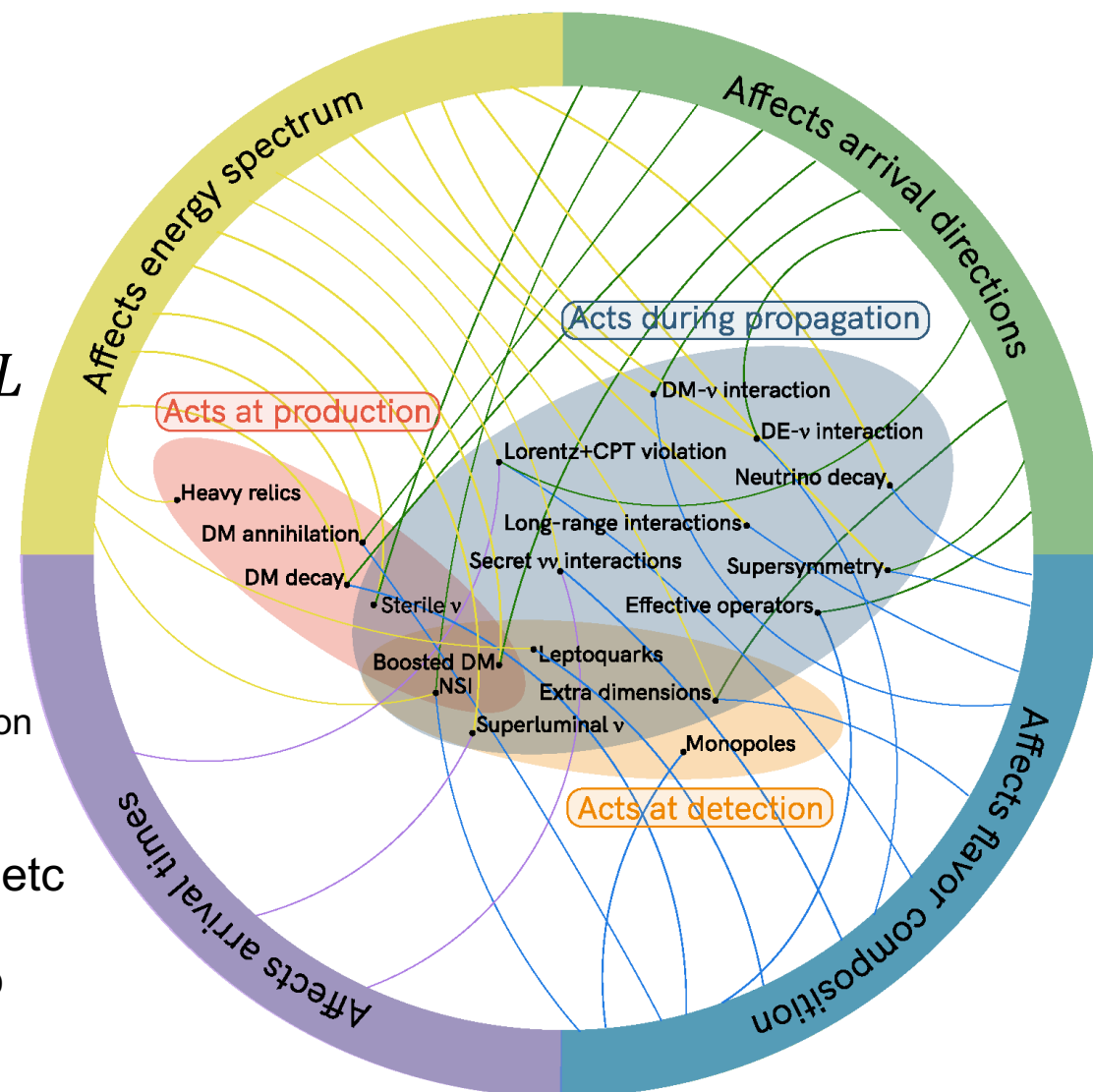
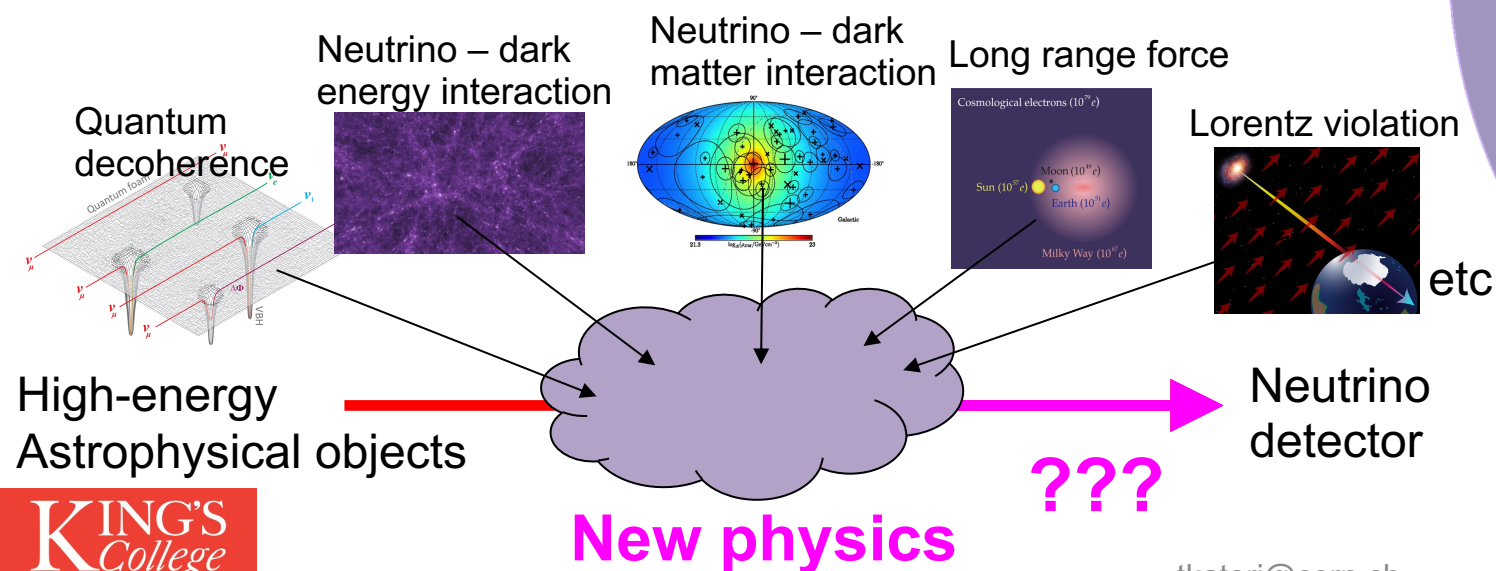
High-energy, long propagating neutrinos

High-energy astrophysical neutrinos

- Long baseline accumulates new physics effect
- High energy enhances new physics effect

$$H \sim \frac{m^2}{2E} + V(\text{new physics}), P \sim V(\text{new physics}) \cdot L$$

- Energy spectrum, arrival time, **flavor** are affected by production, **propagation**, detection of neutrinos



Lorentz violation limits from tabletop to cosmology



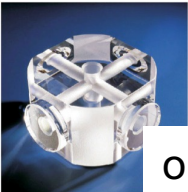
Physics MMA

Lower dimension operators → searches by tabletop experiments
 Higher dimension operators → searches by astrophysical observations

$$H \sim \frac{m^2}{2E} + a^{(3)} - E \cdot c^{(4)} + E^2 \cdot a^{(5)} - E^3 \cdot c^{(6)} \dots$$



torsion pendulum



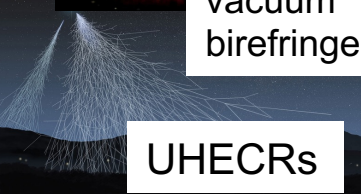
optical resonator



comagnetomator



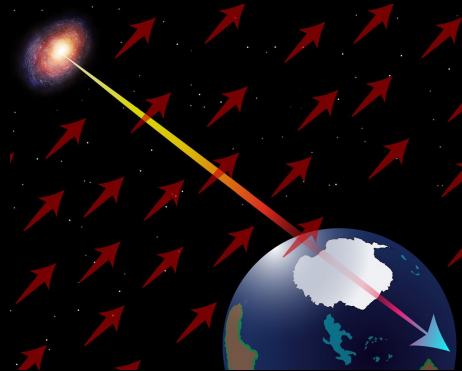
vacuum birefringence



UHECRs

dim.	method	type	sector	limits	ref.
$\frac{a^{(3)}}{a^{(3)}}$	CMB polarization	astrophysical	photon	$\sim 10^{-43}$ GeV	[2]
	He-Xe comagnetometer	tabletop	neutron	$\sim 10^{-34}$ GeV	[3]
	torsion pendulum	tabletop	electron	$\sim 10^{-31}$ GeV	[4]
	muon g-2	accelerator	muon	$\sim 10^{-24}$ GeV	[5]
	neutrino mixing	astrophysical	neutrino	$\sim 10^{-26}$ GeV	[1]
$\frac{c^{(4)}}{c^{(4)}}$	GRB vacuum birefringence	astrophysical	photon	$\sim 10^{-38}$	[6]
	Laser interferometer	LIGO	photon	$\sim 10^{-22}$	[7]
	Sapphire cavity oscillator	tabletop	photon	$\sim 10^{-18}$	[8]
	Ne-Rb-K comagnetometer	tabletop	neutron	$\sim 10^{-29}$	[9]
	trapped Ca^+ ion	tabletop	electron	$\sim 10^{-19}$	[10]
$\frac{a^{(5)}}{a^{(5)}}$	neutrino mixing	astrophysical	neutrino	$\sim 10^{-31}$	[1]
	GRB vacuum birefringence	astrophysical	photon	$\sim 10^{-34}$ GeV ⁻¹	[6]
	ultra-high-energy cosmic ray	astrophysical	proton	$\sim 10^{-22}$ to 10^{-18} GeV ⁻¹	[11]
$\frac{c^{(6)}}{c^{(6)}}$	neutrino mixing	astrophysical	neutrino	$\sim 10^{-37}$ GeV ⁻¹	[1]
	GRB vacuum birefringence	astrophysical	photon	$\sim 10^{-31}$ GeV ⁻²	[6]
	ultra-high-energy cosmic ray	astrophysical	proton	$\sim 10^{-42}$ to 10^{-35} GeV ⁻²	[11]
	gravitational Cherenkov radiation	astrophysical	gravity	$\sim 10^{-31}$ GeV ⁻²	[12]
	neutrino mixing	astrophysical	neutrino	$\sim 10^{-42}$ GeV ⁻²	[1]

Astrophysical neutrino flavour Lorentz violation limits



Weak interaction
 + Small mass
 + Quantum mixing
 = macroscopic quantum system you cannot disturb

L-E plot

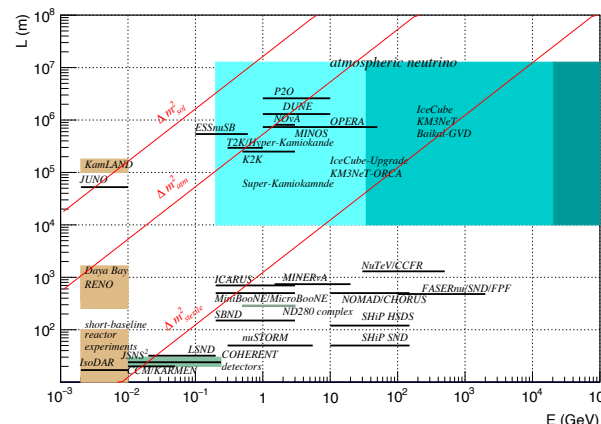
Neutrino telescopes for the ultra-high-energy neutrinos are not Cherenkov detector
 TeV-PeV $\rightarrow$ >100 PeV

High energy, long propagation experiments

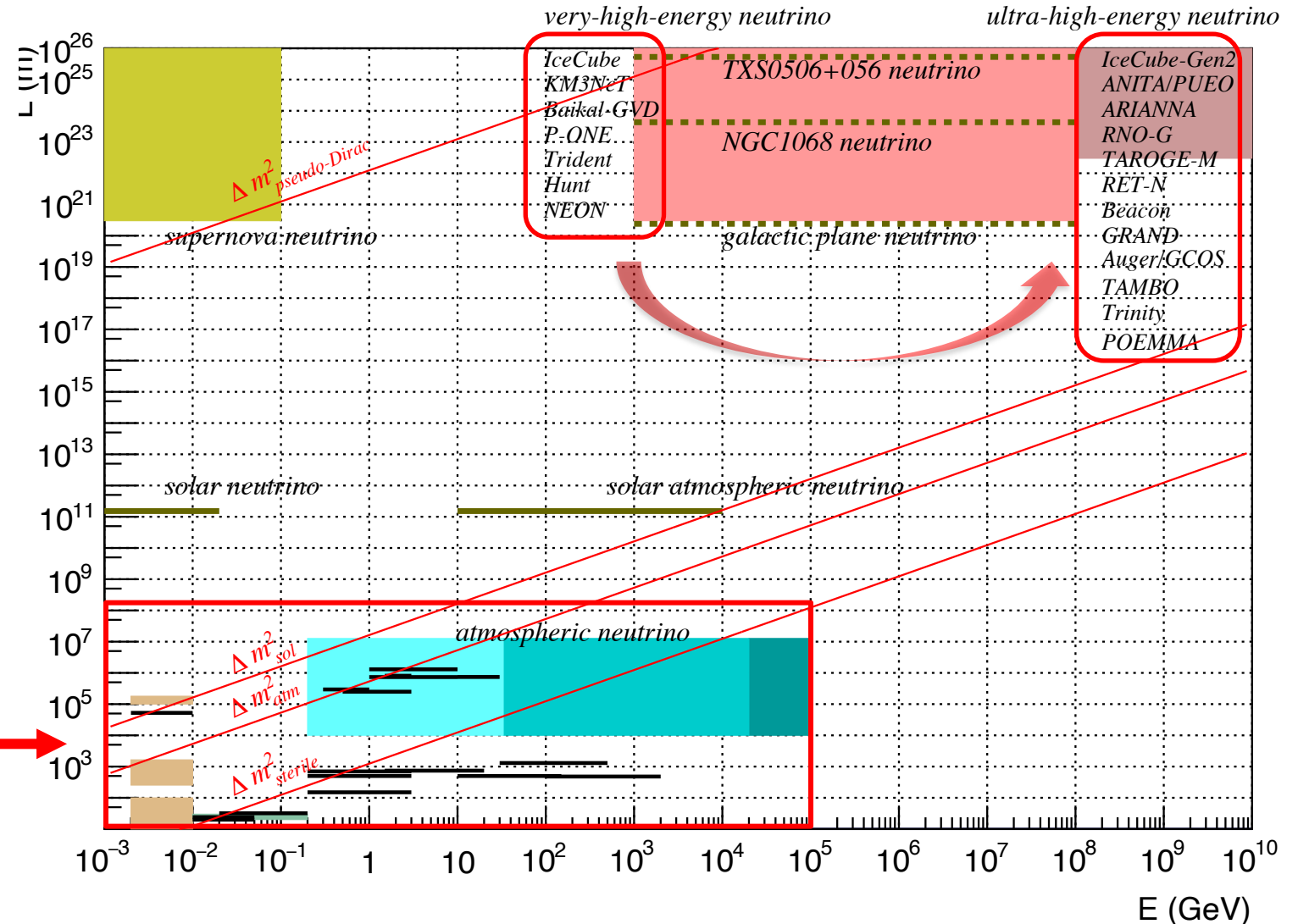
- Neutrino telescopes [Snowmass, JHEA36\(2022\)55](#)

water and ice
 Cherenkov detectors

radio telescope, air
 shower array, etc

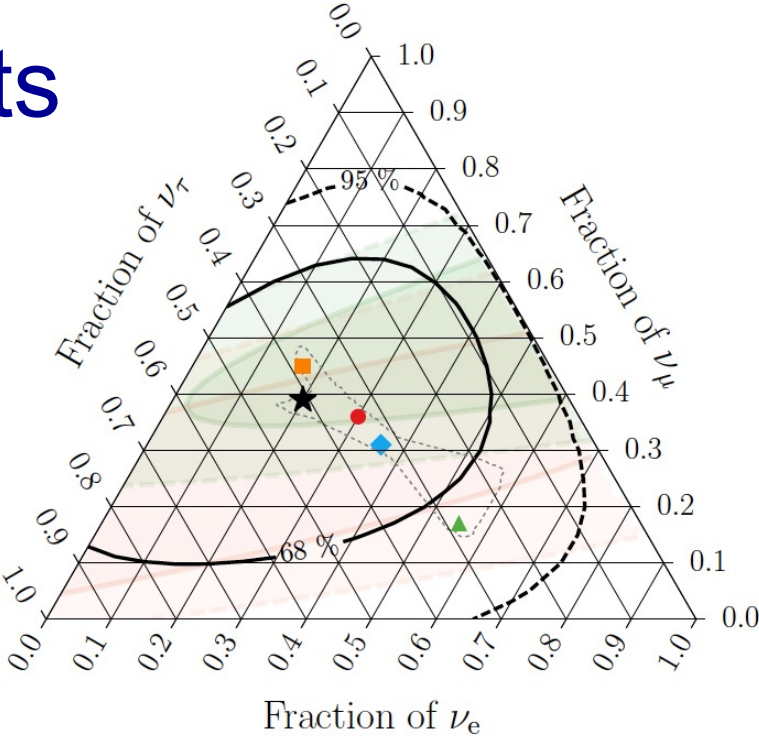
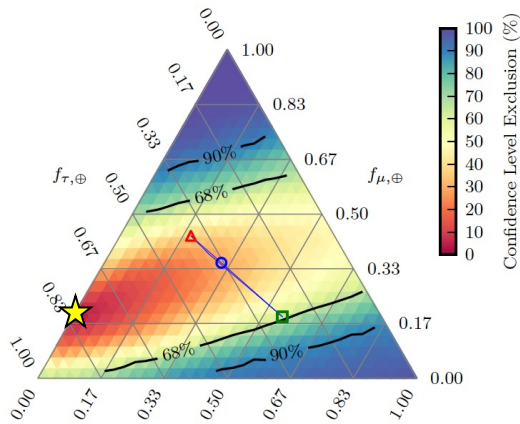


Terrestrial experiments

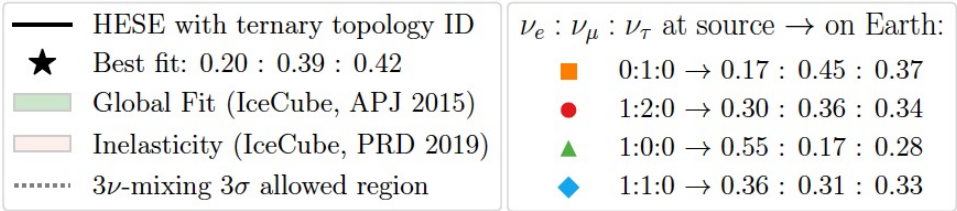


IceCube flavor ratio measurements

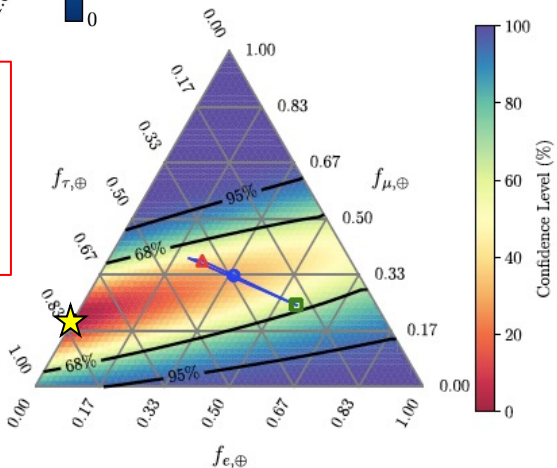
IceCube
1st flavour ratio result
(0.0:0.2:0.8)



IceCube
2nd flavour ratio result
(0.5:0.5:0.0)



IceCube
3rd flavour ratio result
(0.0:0.2:0.8)



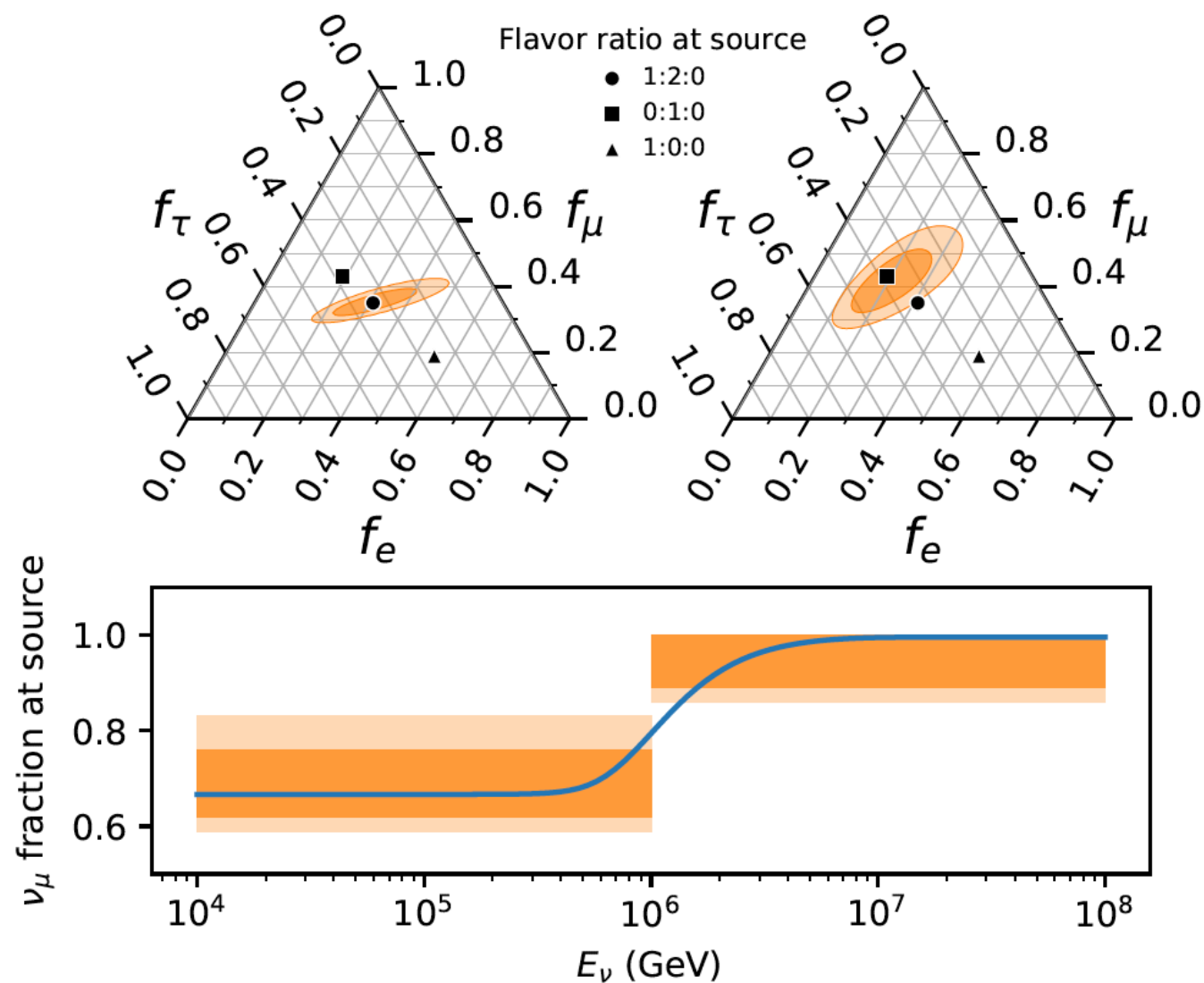
2018 flavour ratio measurement

- Likelihood is very shallow and fit often confuses between ν_e and ν_τ
- Flavour ratio result has some power to distinguish ν_e and ν_τ

Energy dependence of flavor ratio

Muon neutrino increases at higher energy

Future higher-statistics flavor measurement



New physics flavor ratio predictions

New physics models have different flavor ratios

Effective operator

- It includes Lorentz violation
- Assuming all possible standard production models, $(\nu_e:\nu_\mu:\nu_\tau) = (x:1-x:0)$, it covers 2/3 of the phase space.

